



TAMPERE ECONOMIC WORKING PAPERS
NET SERIES

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TRANSITION: OPTIMAL INCOME TAXATION FRAMEWORK

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Working Paper 14
February 2003
<http://tampub.uta.fi/econet/wp14-2003.pdf>

DEPARTMENT OF ECONOMICS
FIN-33014 UNIVERSITY OF TAMPERE, FINLAND

ISSN 1458-1191
ISBN 951-44-5603-3

Understanding the Evolution of Inequality During Transition: The Optimal Income Taxation Framework

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Abstract: What explains the spectacular increases in inequality of disposable income in transitional economies of Central and Eastern Europe? There are at least two possible explanations. First, the pre-tax distribution of income became more unequal because of the shift to a market economy. Second, the degree of progressivity of the income tax system declined. But each of these factors is in turn determined by other structural changes associated with transition—notably, the decrease in public provision of key public goods, the decrease in non income tax revenue sources such as profits from public production, and perhaps a decline in society’s inequality aversion. This paper develops a framework in which these different forces on inequality can be assessed. Using a simple two-type and two-sector optimal income tax model with endogenous wages, we first of all show that a decrease in the provision of public goods could indeed lead to increasing “inherent” inequality, in other words inequality in market incomes. It then deploys the Mirrlees model of optimal non-linear taxation to assess the relative impacts of this increase in inherent inequality, the decreasing sources of non income tax revenue, and possible declines in inequality aversion, to get a numerical feel for their possible impacts on inequality.

Key words: Inequality, optimal redistribution, public provision, transition
JEL numbers: H21, H42, P31

1. Introduction

Tax/transfer system reform was central to the transition process from the centrally planned economy to a market-type economy in Central and Eastern Europe (CEE). In the old fiscal system a large share of tax revenue came directly or indirectly from state-owned firms. The new fiscal system is in turn designed to be compatible with future EU membership of CEE countries. A personal income tax, a value added tax and entrepreneurial profits tax are all largely modelled on western counterparts. The introduction of the new fiscal system, in concert with other structural features of the transition, has had profound indirect and direct distributional effects. One common characteristic of the transition in Central and Eastern Europe has been an increase in income inequality. Both market and disposable income inequality has risen in these countries during the 1990s. Driving this increase in inequality have been a variety of factors. In the pre reform situation the requirement of government expenditure was largely met from non-tax revenue as the profits of public production, taxation of enterprise profits and commodity transactions. Privatisation of state owned firms surely has had significant consequences for income inequality. Other factors such as trade liberalization, changes to the level and composition of government spending including declines in the provision of public goods, and changes in the wage setting process, have all tended to raise inequality. At the same time, it can be argued that these societies have become less averse per se to inequality¹.

This paper develops a framework in which these different forces on inequality can be assessed. We start by surveying the salient empirical facts on income inequality and redistribution based on the Luxembourg Income Study (LIS) database in Section 2. In Section 3 we indicate the potentially important channels for changes in market income inequality, or “inherent” inequality, using a simple two-type and two-sector optimal income tax model with endogenous wages. We argue that a reduction in public goods provision can indeed lead to an increase in inherent inequality in such models. Section 4 accepts an increase in inherent inequality but looks at optimal redistribution in the face of this increase, and also when sources of non income tax revenue disappear as the structure changes, and as aversion to inequality falls—all forces that, it can be argued, have been present in the transition process. Section 5 concludes the paper with a discussion of directions for further research.

¹ According to Atkinson and Micklewright (1992) CEE countries were during the 1970s and 1980s very egalitarian in their disposable income distribution compared with comparable western market economies.

2. The Basic Facts

This section sets the stage by reviewing empirical findings on income inequality and the extent of redistribution in the transition countries.² Data on income distribution shown in Table 1 and 2 are obtained from the LIS. The relatively high quality of this data source has been commented on elsewhere (see Atkinson-Brandolini, 2001) The income concepts employed are market income (MI), social retirement benefits (P) added to market income (MI+P) and disposable income (DI),³ with household size being allowed for by deflating by the square root of the number of household members.

Table 1 provides estimates of the change in the disposable income distribution. In the period considered, the Gini-coefficient of disposable income rose markedly, as did the various decile ratios. Table 2 shows that the inequality of market incomes also rose markedly, a factor confirmed by Table 3, which shows significant increases in the decile ratios of the gross earnings of employees. However, interestingly, Table 2 shows that the extent of redistribution, as measured by the difference in the increase of market income inequality and the increase of disposable income inequality, actually increased.⁴ For example, between 1986 and 1995 in Poland the Gini coefficient for market income increased by over 20 percentage points. But the disposable income Gini only rose by around 10 points. Thus on one measure, the extent of redistribution increased by more than 10 percentage points⁵.

These facts set up our basic analytical questions. What explains the increase in market inequality? Given this increase, what explains the increased degree of redistribution especially if, as is often argued, the degree of inequality aversion also fell during the transition period? The next two sections take up these questions.

² The annual transition report of the European Bank for Reconstruction and Development (EBRD) documents the changes in the transition countries. The most advanced countries in 1997, in terms of EBRD's judgement of progress in these countries, were Czech-Republic, Hungary, Poland, Slovak Republic, Slovenia and Baltic countries. The value of the "transition index" (a summary measure for progress from a planned to a market economy) was greater than 3 and on average the private sectors accounted for over two-thirds (68%) of GDP in these countries. Excluding Baltic countries change in real GDP in these countries between 1989-1997 was -1 %.

³ See Milanovic (2000) p. 375 note 7 and LIS (<http://lisweb.ceps.lu/techdoc.htm>)

⁴ A new personal income tax was introduced in Hungary already in 1988 under the old system. In the beginning the marginal tax rate structure was very progressive with ten bands ranging from 20 to 60%. In 1994 there were six bands rising from 0 to 44% and in 1997 also six bands rising from 20 to 42%. In Czech Republic there were in 1994 six bands ranging from 15 to 44% and in 1997 five bands rising from 15 to 40%. The Polish income tax system in turn differs from those of Hungary and Czech Republic in the sense that there are only three bands (20,32,44 in 1997). (see Table 1 in Piotrowska, 2000)

⁵ According to Milanovic (1998) the average level of social cash transfers as a percent of GDP over the period from the first year of the transition through 1997 was among the highest one in Poland, 17.7 %.

Table 1
Income (disposable) inequality measures

Country	Year	Gini-coefficient	Percentile Ratio(90/10)	Percentile Ratio(90/50)	Percentile Ratio(80/20)
Czech-Republic	1992	20.7	2.37	1.55	1.73
	1996	25.9	3.01	1.79	2.04
Hungary	1991	28.3	3.39	1.82	2.18
	1994	32.3	4.19	2.09	2.42
Poland	1986	27.1	3.51	1.77	2.32
	1992	27.4	3.42	1.84	2.17
	1995	31.8	4.04	1.89	2.37
Russia	1992	39.3	6.66	2.40	3.45
	1995	44.7	9.39	2.82	3.95
Slovak Republic	1992	18.9	2.25	1.49	1.68

Table 2. Gini (G) coefficients and redistribution in transition economies

Country	Year	G(MI)	G(MI+P)	G(DI)	RD*
Czech-Republic	1992	43.7	30.0	21.7	0.50
Hungary	1991	52.0	39.2	30.3	0.42
Poland	1986	39.9	33.5	29.1	0.27
	1992	45.9	36.3	33.8	0.28
	1995	60.6	50.9	38.8	0.36
Russia	1992	56	47.2	45.2	0.19
	1995	62	50.0	48.8	0.21
Slovak Republic	1992	43.0	32.0	20.9	0.51

Source: Milanovic(2000) based on LIS data. * $RD=[G(MI)-G(DI)]/G(MI)$

Table 3 Distribution of gross earnings of employees (P90/P10)

Country	1989	1990	1991	1992	1993	1994	1995	1996	1997
Czech-republic	2.43		2.60	2.75	3.20	3.14	3.70	2.86	2.98
Hungary		3.40		3.56	3.70	3.75			4.17
Poland	2.43		2.85	2.91	3.01	3.40	3.35	3.48	3.53
Russia	3.33	3.36	4.28	8.17	15.55	9.41	9.96	9.60	10.40
Ukraine				3.12	5.51		5.74	5.74	

Source: Flemming-Micklewright (2000), Appendix B

3. Public Provision and Market Inequality

Consider the following model, a modified version of the model in Naito (1999)⁶. There are two types of workers in the economy: Workers of type 1 are less skilled and earn income w_1 . The more skilled workers, type 2, earn a wage $w_2 (> w_1)$. The number of workers of each type is 1. Workers supply labour, denoted by l , and consume two types of goods: a normal private good, x , and a publicly provided good, denoted by g . The latter good is provided by the state sector. Preferences are represented by a strictly monotone, strictly quasi-concave, and twice differentiable utility function by $v(x, l, g)$. Workers maximise $v(x, l, g)$ with respect to his or her labour supply, subject to a given tax schedule, $T(y)$, and the budget constraint $x = y - T(y)$, where $y = wl$ denotes workers gross income.

The good x is produced in the private sector according to an aggregate, constant returns to scale, production function $H(l_1^x, l_2^x, g)$, where l_1^x and l_2^x denote the labour inputs in the private sector. The good g in turn is produced according to the aggregate production function $G(l_1^g, l_2^g)$, where l_1^g and l_2^g are the labour inputs in the public sector. Note that the same technology is used to

⁶ See also Gaube (2000) and Pirttilä-Tuomala (2002)

produce both goods. They have thus similar producer prices as well. For simplicity, the prices for both goods are normalised to unity. This specification captures two important features of the model. First, the wage rates are endogenous in a similar way as in Stern (1982) or Stiglitz (1982). In the

following, $\Omega = \frac{w_1}{w_2}$ depicts the relative wage of the low-skilled type. Assuming a competitive

labour market, Ω is a function of l_1/l_2 , $\frac{w_1}{w_2} = \frac{H_1(l_1, l_2, g)}{H_2(l_1, l_2, g)}$, where H_i ($i=1,2$) denotes the partial

derivatives of the production function with respect to the labour inputs l_i^x . It captures the idea that the relative wage rate of type 1, determined at the market, is a decreasing function of l_1/l_2 . It is

also assumed that the public sector minimizes costs with respect to the (shadow) wages r_1 and r_2 by the government. Thus the public sector minimizes production costs by equating the marginal rate of transformation between unskilled and skilled workers to the ratio of equilibrium wage rates, i.e.

$\frac{r_1}{r_2} = \frac{G_1(l_1, l_2)}{G_2(l_1, l_2)}$, where G_i ($i=1,2$) in turn denotes the partial derivatives of the public sector

production function with respects to labour inputs l_i^g .

Following the standard idea of Pareto-optimal taxation, the government maximises the utility of the less-skilled workers subject to the constraint that the skilled worker must stay at a given utility level. The government redistributes income by taxing income on a non-linear scale. It may also use a uniform public provision of g as a policy variable. We apply the information-based approach to tax policy by assuming that the government can observe the labour income y , but it does not observe the income earning abilities (the wage rates) of the workers. Therefore, the government must select the tax schedule subject to the self-selection constraint that the skilled worker has an incentive to work $l_2 = y_2/w_2$, report income y_2 and consume x_2 instead of wishing to pretend to be the unskilled household, i.e. mimic, working $y_1/w_2 = w_1 l_1/w_2 = \Omega l_1$, reporting income y_1 , and consuming x_1 . The government chooses the optimal tax schedule (or labour – after-tax income) bundles to the two different worker types subject to the constraint that the skilled worker be at a given utility level, the self-selection constraint of the skilled worker, and the resource constraint of the economy ($l_1 = l_1^x + l_1^g$, $l_2 = l_2^x + l_2^g$). We concentrate here on the 'normal' case where the redistribution occurs from the skilled workers to the unskilled ones. Thus the self-selection constraint of the skilled workers is binding. The Lagrangean of the government optimisation problem can be expressed in terms of the controls x_i , l_i , l_i^x , l_i^g ($i = 1,2$)

$$\begin{aligned}
L = & v(x_1, l_1, g) + \delta [v(x_2, l_2, g) - \bar{v}^2] \\
& + \mu [v(x_2, l_2, g) - v(x_1, \Omega l_1, g)] \\
& + \rho_x [H(l_1^x, l_2^x, g) - x_1 - x_2] \\
& + \rho_g [G(l_1^g, l_2^g) - 2g] + \alpha_1 [l_1 - l_1^x - l_1^g] + \alpha_2 [l_2 - l_2^x - l_2^g]
\end{aligned} \tag{1}$$

The first-order conditions are the following:

$$x_1 : v_x^1 - \mu \hat{w}_x^2 - \rho_x = 0, \tag{2}$$

$$l_1 : v_l^1 - \mu \hat{w}_l^2 \left(\frac{\partial \Omega}{\partial l_1} l_1 + \Omega \right) + \alpha_1 = 0, \tag{3}$$

$$x_2 : (\delta + \mu) v_x^2 - \rho_x = 0, \tag{4}$$

$$l_2 : (\delta + \mu) v_l^2 + \alpha_2 = 0, \tag{5}$$

$$l_i^x : \rho_x H_i - \mu \hat{w}_l^2 \Omega_i l_i - \alpha_i = 0, i = 1, 2, \tag{6}$$

$$l_i^g : \rho_g G_i - \alpha_i = 0, \tag{7}$$

where the hat terms refer to the so-called mimickers, i.e. type 2 workers when mimicking the choice of type 1 and $\Omega_i = \frac{\partial \Omega}{\partial l_i^x}, i = 1, 2$.⁷

Suppose that the government has chosen to produce a certain amount of consumption, g . Given this, suppose further that the government's income tax and public employment policy is optimal. We will now show that the marginal rate of transformation between these two types of labour in public production is smaller than that one in the private sector, i.e. $\frac{r_1}{r_2} < \frac{w_1}{w_2}$.

From the equation (6) we see that only in the case that the second term is zero the production efficiency holds i.e. $G_1/G_2 = H_1/H_2$. But we also note that the term $-\mu \hat{w}_l^2 l_i$ is positive. Thus the Diamond-Mirrlees efficiency theorem does not hold in this model. Given our assumptions about the

⁷ The function Ω is homogeneous of degree zero in (l_1^x, l_2^x) . It implies $\Omega_1 < 0$ and $\Omega_2 > 0$.

public production function (6) implies the following result; to produce a given amount of consumption the government should employ more unskilled workers and less skilled workers than is necessary to minimize cost at the prevailing gross wage rates. This means that if the supply of low skilled workers becomes scarcer in the private sector, through hiring more of these workers into the public sector, this reduces the wage differentials of the workers. Thus, indirect redistribution through public sector employment will Pareto-improve welfare by mitigating the incentive problem of the non-linear income tax system. Or put it in terms of envelope arguments. If in the beginning the production efficiency holds, then the marginal change in hiring more low skilled workers to the public sector has no first order welfare costs. It affects only relative wages of the low skilled workers.

Given the optimal income tax and employment policy, we may also use the envelope argument to detect the change in the social welfare from an increase in the level of the publicly provided good as follows:

$$\frac{dL}{dg} = v_g^1 + (\delta + \mu)v_g^2 - \mu\hat{w}_g^2 + \rho_x H_g - \mu\hat{w}_l^2 \frac{d\Omega}{dg} l_1 - 2\rho_g. \quad (8)$$

Our focus is, however, more in the production side of the economy, and therefore we concentrate on the case with the weakly separable (between consumption and labour (or leisure)) utility function. Rewriting (8) by substituting for ρ_x from (2) and (4) yields

$$\frac{dL}{dg} = \rho_x H_g - \mu\hat{w}_l^2 \frac{d\Omega}{dg} l_1. \quad (9)$$

What is interesting in (9) is the link between the publicly provided private good and the wage structure of the economy (the term $-\mu\hat{w}_l^2 \frac{d\Omega}{dg} l_1$). If its provision leads to a relative increase in the wage rate for type 1 workers, then indirect redistribution through public provision will Pareto-improve welfare by mitigating the incentive problem of the non-linear income tax system.

These results bear resemblance to the interesting recent findings by Naito (1999) that if wage rates are endogenous, redistribution devices that otherwise would not be applied – in Naito's case public inputs and commodity taxation and in our case public sector employment combined with public provision of goods – become welfare-improving. These theoretical results support the view

that the privatisation and a decrease in public provision such as education, health care and social services may have been important factors in explaining increasing inherent inequality in transition economies during the 1990s⁸.

4. Optimal Non-linear Redistribution

An analytical framework for thinking through the relationship between inherent inequality and the extent of redistribution is put forward by James Mirrlees in his Nobel Prize winning paper (Mirrlees, 1971). It captures the central features in thinking about the evolution of redistribution policy. Certain key elements of the Mirrlees model are useful for our purposes. First is the concept of inherent inequality reflecting among other things skilled /unskilled wage differentials, asset inequality and social norms. If there is no intervention by the government, the inherent inequality will be fully reflected in the disposable income. However, if the government wants to intervene – as seems to be the case in the transition countries – it will find the second component of the Mirrlees model, the egalitarian objectives of the government. And if the government tries to redistribute income from high-income people to low-income people, there will be incentive and disincentive effects. In other words the redistribution policy is the product of circumstances and objectives. Finally, the Mirrlees model has a revenue requirement from the tax/transfer system, to finance an exogenously given level of public goods. In this framework, we use numerical simulations to study questions such as how optimal redistribution might respond when inherent inequality increases, the government becomes less averse to inequality and the role of non-tax revenue decreases.⁹

It is useful to lay out the basic model, even though it is well known. There is a continuum of individuals, each having the same preference ordering, which is represented by an additive utility function $u = U(x) - V(l)$ defined over consumption x and hours worked l , with $U_x > 0$ and $V_l < 0$ (subscripts indicating partial derivatives) and where $V(\cdot)$ is convex. Workers differ only in

⁸ As pointed out to us by Roger Gordon a publicly owned firm may acquire information about the hourly wages of its workers. Given this information redistribution towards to less skilled workers will be cheaper than when done outside public sector.

⁹ These questions were examined by Newbery (1997) in the framework of optimal linear taxation.

the pre-tax wage w they can earn. There is a distribution of w on the interval (s, h) represented by the density function $f(w)$. Gross income $y = wl$.

Suppose that the aim of policy can be expressed as maximizing the following social welfare criterion

$$S = \int_s^h W(u(w))f(w)dw, \quad (10)$$

where $W(\cdot)$ is an increasing and concave function of utility. The government cannot observe individuals' productivities and thus is restricted to setting taxes and transfers as a function only of earnings, $T[y(w)]$. The government maximizes S subject to the revenue constraint

$$\int_s^h (y(w) - x(w))f(w)dw = R \quad (11)$$

where in the Mirrlees tradition R is interpreted as the required revenue for essential public goods. The more non-tax revenue a government receives from external sources (as in the old fiscal system from state owned firms), the lower is R . In addition to the revenue constraint, the government faces incentive compatibility constraints. These in turn state that each w -individual maximizes utility by choice of hour. Totally differentiating utility with respect to w , and making use of workers utility maximization condition, we obtain the incentive compatibility constraints,

$$\frac{du}{dw} = -\frac{lV_l}{w}. \quad (12)$$

Since $T = wl - x$, we can think of government as choosing schedules $l(w)$ and $x(w)$. In fact it is easier to think of it choosing a pair of functions, $u(w)$ and $l(w)$, which maximize welfare index (10) subject to the incentive compatibility condition (12) and the revenue requirement (11). Omitting details (for an exposition see Tuomala, 1990), the first order conditions of this problem imply a pattern of marginal rates¹¹, $t(y) = T'(y)$, satisfying

¹⁰ The 1.order condition of individual's optimisation problem is only a necessary condition for the individual's choice to be optimal, but we assume here that it is sufficient as well. Assumptions that assure sufficiency are provided by Mirrlees (1976). Note also that while we here presume an internal solution for l , (12) remains valid even if individuals were bunched at $l=0$ since, for them, $du/dw=0$.

¹¹ There are other works that have looked at alternative derivations and formulae for non-linear taxation, see Revesz (1989), Roberts (2000) and Saez (2001)

$$\frac{t}{1-t} = (E^{-1} + 1)U_x \mu(w) / \lambda w f(w) \quad (13)$$

where λ is the multiplier on the revenue constraint and

$$\mu(w) = \int_s^w ((W'U_x - \lambda)(1/U_x))f(p)dp. \quad (14)$$

is the multiplier on the incentive compatibility constraint. This latter satisfies the transversality conditions

$$\mu(s) = \mu(h) = 0. \quad (15).$$

Finally, as in Atkinson-Stiglitz (1980) $E = V'/V$. It is the elasticity of labour supply with respect to net wage, holding marginal utility of income constant, i.e. E is “compensated” wage elasticity in a rather unusual sense.

Unfortunately, however, as is well recognized in the non-linear taxation literature, closed form analytical results are few and far between.^{12 13} It should be clear from (13) that the variation of the optimal marginal tax rate with the level of income is a complex matter, and that comparative statics of inequality and averages as parameters vary will not be available in closed form. This is a general feature on the optimal non-linear income taxation literature (see Tuomala, 1990) where, following the lead of Mirrlees (1971) numerical calculations have proved useful in generating

¹² Equations (13) - (15) lead to the few qualitative conclusions available in this framework (see Tuomala, 1990). It can be shown that the marginal tax rate on income is nonnegative. This is more striking than it at first looks. It may very well be optimal to have the average tax rate less than zero, but it is never optimal to subsidize earnings at margin. An intuition is that it is cheaper to get people to given indifference curve by reducing average rate rather than by exacerbating deadweight loss through distorting their labour supply decisions. It can also be shown that the marginal tax rate is less than one. We also have the famous "end point" results. If wage distribution is bounded above, then the marginal tax rates at the top is zero. If it is optimal for least able individual to work then the marginal tax rate on least able is zero. An intuition behind these endpoint results is that only reason to have a marginal tax rate differing from zero is to raise an average tax rate above that point and lower it below i.e. equity considerations. But at the top is no one to take from and at the bottom there is no one to give to. So at the end points only efficiency considerations matter. Numerical solutions (Tuomala, 1990) have shown, however, that these results have very little practical relevance.

¹³ There is a special case in which a closed-form solution can be obtained. This possibility was first shown by Lollivier and Rochet (1983) when preferences are quasi-linear in leisure and the social welfare function is utilitarian. Properties of the solution for this case were studied by Weymark (1986) for the discrete case and Ebert (1992) for the continuous case. Boadway et al (2000) provide a full characterization of the solution when preferences are quasi-linear in leisure. Diamond (1998) in turn shows that when preferences are quasi-linear in consumption, an explicit expression for the marginal rate can be derived in terms of the distribution of ability, the elasticity of the labour supply and the form of the social welfare function. He finds the marginal tax rate schedule to be u-shaped in his example. Dahan and Strawczynski (2000) clarify this result showing that a rising marginal rates at high incomes depend on the joint assumptions of an unbounded distribution and quasi-linear preferences.

useful results¹⁴. We follow this route here. With these techniques, we can compute post tax income at each level of w , and thus calculate inequality of pre and post tax income as well as total income, for different values of key parameters. Our focus is on identifying the combined effects of greater inherent inequality (the standard deviation of w), smaller inequality aversion and larger tax revenue requirement. We turn now to this task.

We assume w to be distributed lognormally with parameters m and σ (see Aitchison and Brown, 1957). This assumption is common in the literature, following Mirrlees (1971). For numerical simulations we choose $\sigma = 0.39, 0.5, 0.7$ and 1 and $m = -1$ (and -0.8)¹⁵. The utility function $u(\cdot)$ has the constant elasticity of substitution form

$$u(x, l) = \left[(1 - \phi)x^{-a} + \phi(1 - l)^{-a} \right]^{-1/a} \quad (16)$$

where the elasticity of substitution between consumption and leisure $\varepsilon = 1/(1+a)$. Where $\varepsilon < 1$, the labour supply function is backward sloping. Stern (1976) pays special attention to the question of how to relate the assumptions about labour supply to econometric research on labour supply behaviour.¹⁶ He reports estimates of the labour supply (uncompensated) elasticity ranging from -0.07 to -0.30 , with a central value of -0.15 , and corresponding estimates of elasticity of substitution ε from 0.75 to 0.2 , with preferred value of 0.4 . Our calculations were carried out for the cases $\varepsilon = 0.4$ ($a=1.5$), $\varepsilon = 0.5$ ($a=1$), $\varepsilon = 0.66$ ($a= 0.5$) and $\varepsilon = 1$ (Cobb-Douglas case, $u=\ln x+\ln(1-l)$). Hence we also extend previous numerical simulations in the framework of non-linear income taxation. The social welfare function of the government is specified¹⁷ as $W(u) = -\frac{1}{\beta} e^{-\beta u}$ so that β measures the degree of inequality aversion in the social welfare function of the government (in the case of $\beta = 0$, we define $W = u$). $R = 1 - \int x(w)f(w)dw / \int y(w)f(w)dw$ is specified as a fraction of national income, and is assumed to vary between -0.1 and 0.1 .

¹⁴Tuomala (1990) gives details of the computational procedure.

¹⁵ As in Kanbur-Tuomala (1994) we also try to calibrate the lognormal distribution so that the income distribution inferred from the ability distribution matches the actual one. Of course it would be important to solve marginal tax rate formula using the empirical earnings distribution. This is not possible to make directly because the earnings distribution is affected by the tax schedule itself. Saez (2001) makes an important innovation in this question. He calibrates the ability distribution so that given the utility function chosen and the actual tax schedule the resulting pre tax distribution replicates the empirical earnings distribution.

¹⁶ Unfortunately we are not aware of any econometric labour supply study in transition countries.

¹⁷For further discussion on the transformation of each individual's utility see Tuomala (1990)

Table 4 (“The old fiscal sytem”)

$\varepsilon=0.5 \quad \beta=1 \quad \sigma=.39 \quad m=-1$									
F(w)	R=-.1				R=0.0				
	x	y	MTR%	u	x	y	MTR%	u	
0.10	0.17	0.09	62	-7.63	0.16	0.10	65	-8.10	
0.50	0.20	0.18	56	-6.85	0.19	0.19	59	-7.24	
0.90	0.27	0.32	45	-5.78	0.26	0.33	47	-6.06	
0.99	0.38	0.49	28	-4.78	0.36	0.50	29	-4.99	
RD	0.55				0.51				
Decile ratio (P90/P10)	1.59	3.5			1.63	3.3			

RD = the extent of redistribution

Table 5 (“The old fiscal system”)

$\varepsilon=1 \quad \beta=1 \quad \sigma=.39 \quad m=-1$									
F(w)	R=-.1				R=0.0				
	x	y	MTR%	u	x	y	MTR%	u	
0.10	0.11	0.08	30	-2.68	0.10	0.07	33	-2.57	
0.50	0.17	0.15	28	-2.39	0.15	0.15	30	-2.30	
0.90	0.27	0.28	24	-2.00	0.25	0.28	25	-1.94	
0.99	0.41	0.44	20	-1.64	0.38	0.45	18	-1.60	
RD	0.31				0.37				
Decile ratio (P90/P10)	2.48	3.58			2.50	3.97			

Table 6a (“The new fiscal system”)

$\varepsilon=0.5$	$\sigma=0.5$	$m=-1$							
F(w)	R=0.0				R=0.0				$m=-.8$
	x	y	MTR%	u	x	y	MTR%	u	
0.10	0.15	0.10	51	-8.67	.18	.11	50	-7.44	
0.50	0.20	0.20	50	-7.13	.24	.24	48	-6.17	
0.90	0.29	0.37	45	-5.58	.35	.43	43	-4.94	
0.99	0.49	0.59	38	-4.33	.51	.68	35	-3.85	
RD	0.48				.50				
Decile ratio (P90/P10)	1.93		3.7		1.90		3.83		

Table 6b (“The new fiscal system”)

$\varepsilon = 1$	$\beta = 0$	$\sigma=0.5$	$m=-1$	
F(w)	R=0.0			
	x	y	MTR%	u
0.10	0.09	0.06	30	-2.79
0.50	0.15	0.15	29	-2.59
0.90	0.24	0.32	26	-2.05
0.99	0.47	0.57	22	-1.41
RD	0.45			
Decile ratio (P90/P10)	2.9	5.3		

Table 7 (“The new fiscal system”)

$\varepsilon=0.5$	$\beta=0$	$\sigma=.7$	$m=-1$						
				R=0.0		R=.1			
F(w)	x	y	MTR%	u	x	y	MTR%	u	
0.10	0.16	0.06	56	-7.89	0.14	0.06	60	-8.86	
0.50	0.20	0.17	60	-6.89	0.19	0.18	63	-7.22	
0.90	0.31	0.45	57	-4.95	0.30	0.47	60	-5.41	
0.99	0.54	0.91	45	-3.79	0.55	0.96	37	-3.85	
RD	0.74				0.73				
Decile ratio (P90/P10)	1.94	7.56			2.14	7.91			

Table 8 (“The new fiscal system”)

$\varepsilon=.5.$	$\beta=0$	$\sigma=1.$	$m=-1$						
				R=0.0		R=.1			
F(w)	x	y	MTR%	u	x	y	MTR%	u	
0.10	0.17	0.02	55	-7.69	0.16	0.02	59	-7.55	
0.50	0.21	0.14	68	-6.35	0.20	0.15	71	-6.67	
0.90	0.35	0.55	71	-4.65	0.33	0.61	72	-4.88	
0.99	0.70	1.61	58	-3.21	0.67	1.65	59	-3.31	
RD	0.92				0.93				
Decile ratio (P90/P10)	2.06	27.5			2.06	30.1			

Table 9 (“The new fiscal system”)

$\varepsilon=0.66$	$\beta=0$	$\sigma=0.5$	$m=-1$		$\varepsilon=0.4$	$\beta=0$	$\sigma=0.5$	$m=-1$
F(w)	x	Y	MTR%	u	x	y	MTR%	u
0.10	0.13	0.09	41	-4.11	0.17	0.10	58	-17.41
0.50	0.19	0.18	40	-3.69	0.21	0.20	58	-13.75
0.90	0.29	0.35	35	-3.26	0.29	0.38	52	-9.74
0.99	0.45	0.58	28	-2.89	0.42	0.61	39	-6.73
RD	0.45				0.54			
Decile ratio (P90/P10)	2.23	4.08			1.70	3.70		

Tables 4-9 give net income (x), gross income (y), optimal marginal tax rates (MTR) and utility levels (u) at various percentiles of the ability distribution.¹⁸ Tables 4 and 5 reflect "the old fiscal system" ($\beta = 1$, $\varepsilon = 0.5$ or 1 , $\sigma = 0.39$, $R = -0.1, 0.0$) and tables 6a b, 7, 8 and 9 in turn "the new one" ($\beta = 0$, $\varepsilon = 0.5$ or 1 , $\sigma = 0.5, 0.7$ and 1 , $R = 0.0, 0.1$). Tables 4-9 also provide the decile ratio (P90/P10) for net income and gross income. Unlike the scalar inequality measures the use of fractile measures such as the decile ratio allows us to consider changes in inequality at various different points in the distribution. Since marginal tax rates may be a poor indication of the redistribution powers of an optimal tax structure we measure the extent of redistribution as the proportional reduction between the decile ratio for market income, y, and the decile ratio for disposable income, x,

Consider first the progressivity of the tax structure as a function of market inequality and revenue requirement. Tables 4-9 show that optimal tax/transfer systems become more progressive when inequality increases, $\sigma = 0.5$, $\sigma = 0.7$ and $\sigma = 1.0$, and when R becomes more negative (i.e. more non tax revenue). To understand this, we can combine the results of two earlier studies. Kanbur-Tuomala (1994) show that with greater market income “inherent” inequality optimal marginal tax rates increase with income over the majority of the population. On the other hand we know from Immonen-Kanbur-Keen-Tuomala (1998) that as the revenue requirement becomes negative so that for example non-tax revenue

¹⁸ With the utility function we use, there is “bunching”—all those below a critical value of w choose not to work. Their pre tax income is thus zero and their post tax income is whatever the optimal tax and transfer regime gives them.

is available the minimum income requirement for the poor can be met without clawing back revenue with a high marginal tax rate. Thus we have low marginal tax rates on the poor. In other words, optimal progressivity, taking into account incentive effects, increases with higher inherent inequality and with non-tax revenue. Thus, while the increasing inherent inequality would have induced a partially correcting “optimal” increase in progressivity of the tax/transfer system, the decrease in non-tax revenue (and hence increase in the revenue requirement from the tax system) that was also seen in the transition would have been a force for decreasing progressivity.

In tables 4-9 we see what happens when the government becomes less averse to inequality, inherent inequality increases and the revenue requirement also increases. Figure 1 shows the relationship between the extent of optimal redistribution, RD, and the wage dispersion, σ , in the case of ($\beta = 0$, $\varepsilon = 0.5$, $R = 0.0$). The effects of varying inequality aversion, β , from 0 to 1 and maximin can be seen in Figure 2, plotted for a distribution $\sigma = 0.39$. The extent of optimal redistribution increases as a consequence of increasing the wage dispersion. This is just what we can see in those transition countries having at least two observations (see table 2). On the other hand the pattern of marginal tax rates is quite different. With parameters ($\varepsilon = 0.5, \sigma = 0.7$, $\beta = 0$, $R = 0.0$) the marginal tax rate increases with income up to the 74 %; with $\varepsilon = 1.0$, on the other hand, it increases with income up to 69 %. An interesting question is when might an increase in inherent inequality, an increase in the tax revenue requirement, and a decrease in inequality aversion, be roughly offsetting? We see in tables 5 and 6b ($\varepsilon = 1$) that in terms of marginal tax rate structure the effect of increasing the wage dispersion from $\sigma = 0.39$ to $\sigma = 0.5$ is the same as moving from $\beta = 1$ to $\beta = 0$. If the extent of redistribution is the criterion then the cases ($\varepsilon = 0.5$, $\beta = 1$, $\sigma = 0.39$, $R = 0.0$) (table 6a) and ($\varepsilon = 0.5$, $\beta = 0$, $\sigma = 0.5$, $m = -0.8$, $R = 0.0$) (table 6a) are roughly speaking the same. Thus given this criterion the effect of increasing the inherent inequality from $\sigma = 0.39$ to $\sigma = 0.5$ (and $m = -1$ to $m = -0.8$), is the same as moving from $\beta = 1$ to $\beta = 0$. In other words if market income inequality has risen as much as represented by this move, then it would need a considerable decrease in concern for equity to offset the case for the same extent of redistribution. If we in turn change the elasticity of substitution, ε , then the cases ($\varepsilon = 0.5$, $\beta = 1$, $\sigma = 0.39$, $R = 0.0$) and ($\varepsilon = 0.4$, $\beta = 0$, $\sigma = 0.5$, $R = 0.0$) produce the same extent of redistribution. The table 10 summarizes how the extent of redistribution varies with the wage dispersion in different cases.

Table 10 The extent of redistribution, RD, (%)

	σ		
	0.39	0.5	0.7
$(\beta=1, \varepsilon=0.5, R=-0.1)$	55	67	84
$(\beta=1, \varepsilon=0.5, R=0.0)$	51	65	84
$(\beta=0, \varepsilon=0.4, R=0.0)$	39	54	75
$(\beta=0, \varepsilon=0.5, R=0.0)$	34	50	74
$(\beta=0, \varepsilon=0.5, R=0.1)$	31	48	73
$(\beta=0, \varepsilon=0.66, R=0.0)$	29	45	72

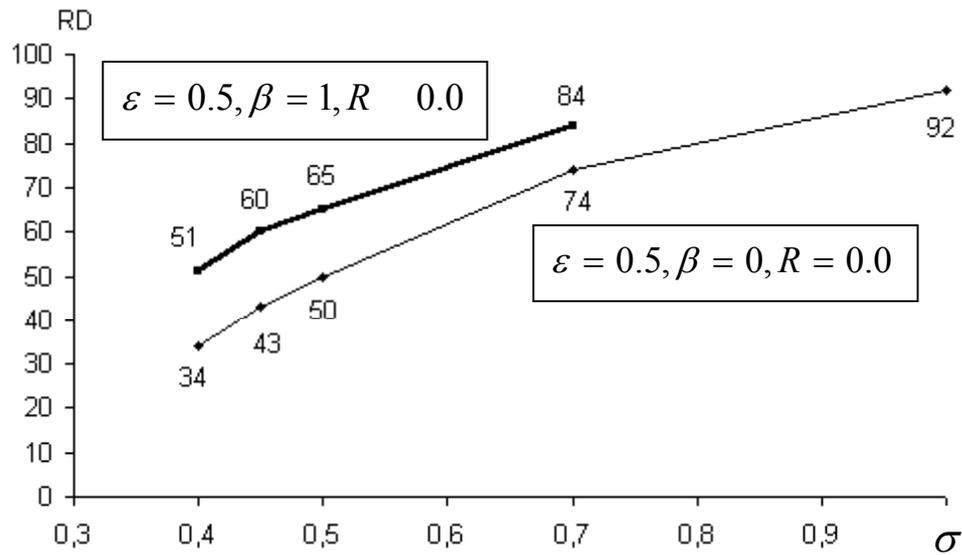


Figure 1 The graph shows how the extent of redistribution varies with the wage dispersion

RD

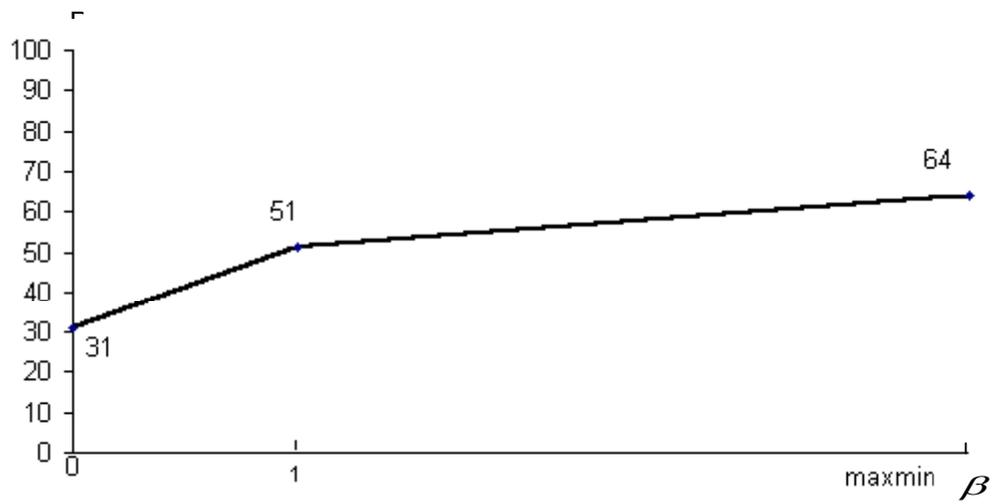


Figure 2 The graph shows how the extent of redistribution varies with inequality aversion. Other parameters are fixed as follows ($\varepsilon=0.5, \sigma=0.39, R=0.0$)

5. Conclusions

In this paper we argue that an analysis of the evolution of pre and post tax income inequality in the transition economies of Central and Eastern Europe can be structured, and the different forces in play understood, through the framework of optimal income taxation. Using the simple two-type and two-sector optimal income tax model we first of all show that the privatisation and a decrease in public provision of public goods may have been an important factor in explaining increasing pre-tax (“inherent”) inequality in transition economies during the 1990s. We also ask, in the framework of non-linear optimal tax theory, how redistribution might respond when inherent inequality increases, the government becomes less averse to inequality and the role of non-tax revenue decreases, all of which happened during transition. We use numerical simulations to study these questions. We discuss when these forces are offsetting and when they reinforce each other as governments choose tax/transfer schedules optimally in response to them, in trying to understand the stylised facts of pre and post tax income inequality during transition. While the increase in inherent inequality induces a response of greater progressivity, this is counteracted by the tendency of the other two forces to decrease progressivity. Overall “optimal” progressivity thus increases, but not sufficiently to overcome the increase in inherent inequality, which leads to an increasing post tax inequality. And these are precisely the stylised facts of inequality and progressivity during transition that we set out to investigate.

References

- Aitchison, J. & Brown, J.A.C.(1957), *The lognormal distribution with special reference to its uses in economics*, Cambridge University Press,
- Atkinson, A.B. & Stiglitz, J.E. (1980), *Lectures on public economics*, McGraw-Hill.
- Atkinson, A.B. & Micklewright, J. (1992), *Economic transformation in Eastern Europe and the distribution of income*, Cambridge University Press.
- Atkinson, A.B. & Brandolini (2001), Promise and Pitfalls in the use of ‘secondary’ data-sets. Income inequality in OECD countries as a case study, *Journal of Economic Literature*, 39:3, 771-800.
- Boadway, R., Cuff, K and M. Marchand, (2000) Optimal income taxation with quasi-linear preferences revisited, *Journal of Public Economic Theory*.
- Diamond, P. (1998), Optimal income taxation: an example with a U-shaped pattern of optimal marginal tax rates, *American Economic Review*.
- Dahan, M. & Strawczynski M. (2001), The optimal non-linear income tax, *American Economic Review*.
- Ebert,U. (1992), A re-examination of the optimal nonlinear income tax, *Journal of Public Economics* 49,47-73.
- Flemming. J &J. Micklewright (2000), *Income Distribution, Economic Systems and Transition*, Handbook of income distribution, vol 1 eds. A.B.Atkinson & F. Bourguignon, North-Holland.
- Gaube, Thomas, (2000) *Income taxation and production efficiency in a simple two-sector economy* , Bonn Econ Discussion papers, 14/2000.
- Immonen, R.,Kanbur, R.,Keen, M. & Tuomala, M. (1998), Tagging and taxing: The optimal use of categorical and income information in designing tax/transfer schemes, *Economica*.
- Kanbur, R. & Tuomala, M. (1994), Inherent inequality and the optimal graduation of marginal tax rates, *Scandinavian Journal of Economics* 96 (2), 275-282.
- Lollivier, S-Rochet, J-C (1983), Bunching and second order conditions: a note on optimal tax theory, *Journal of Economic Theory* 31, 392-400.
- Milanovic, B (2000), The median–voter hypothesis, income inequality, and income redistribution: an empirical test with the required data, *European Journal of Political Economy* vol 16, 367-410.
- Milanovic, B (1998), *Income, inequality and poverty during the transition from planned to market economy*, World Bank Regional and Sectoral Studies, Washington, DC:World Bank.
- Mirrlees,J.A. (1971), An exploration in the theory of optimum income taxation, *Review of Economic Studies* 38, 175-208.
- Mirrlees, J.A. (1976), Optimal tax theory : A synthesis, *Journal of Public Economics* 6, 327-58,.

- Newbery, D. (1997), Optimal tax rates and tax design during systemic reform, *Journal of Public Economics* 63,177-206.
- Naito, H. (1999), Re-examination of uniform commodity taxes under a non-linear income tax system and its implication for production efficiency, *Journal of Public Economics* 71, 165-188.
- Piotrowska,M, (2000), Taxes and transfers as instruments influencing income inequality in transition countries, ISQOLS-conference, Girona, Spain.
- Pirttilä,J and M.Tuomala (2002), Publicly provided private goods and redistribution; A general equilibrium analysis, *Scandinavian Journal of Economics* 104(1),173-188.
- Revesz,J. (1989), The optimal taxation of labour income, *Public Finance* 44, 453-75.
- Roberts,K. (2000), A reconsideration of optimal income tax, in *Incentives, Organization and Public Economics*, papers in Honour of Sir James Mirrlees, eds by P.Hammond and G.Myles, Oxford University Press.
- Saez, E. (2001), Using elasticities to derive optimal income tax rates, *Review of Economic Studies* 68, 205-229.
- Stern, N (1982), Optimal taxation with errors in administration, *Journal of Public Economics* 17,181-211.
- Stiglitz,J.E. (1982) , Self-selection and Pareto-efficient taxation, *Journal of Public Economics* 17, 213-240.
- Tuomala, M.(1984), On the optimal income taxation: some further numerical results, *Journal of Public Economics* 23, 351-66.
- Tuomala, M. (1990), *Optimal income tax and redistribution*, Clarendon Press, Oxford.
- Weymark, J. (1986) A reduced-form optimal nonlinear income tax problem, *Journal of Public Economics* 30,199-217.