

Doping a bad metal: Origin of suppression of the metal-insulator transition in nonstoichiometric VO₂

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Rutile (*R*) phase VO₂ is a quintessential example of a strongly correlated bad metal, which undergoes a metal-insulator transition (MIT) concomitant with a structural transition to a V-V dimerized monoclinic (*M*₁) phase below $T_{\text{MIT}} \sim 340$ K. It has been experimentally shown that one can control this transition by doping VO₂. In particular, doping with oxygen vacancies (*V*_O) has been shown to completely suppress this MIT *without* any structural transition. We explain this suppression by elucidating the influence of oxygen vacancies on the electronic structure of the metallic *R* phase VO₂, explicitly treating strong electron-electron correlations using dynamical mean-field theory (DMFT) as well as diffusion Monte Carlo (DMC) flavor of quantum Monte Carlo (QMC) techniques. DMC calculations show a gap closure in the *M*₁ phase when vacancies are present, suggesting that when vacancies are introduced in the high-temperature rutile phase, the dimerized insulating phase cannot be reached when temperature is lowered. Both DMFT and DMC calculations of nonstoichiometric metallic rutile phase shows that this tendency not to dimerize in the presence of vacancies is because *V*_O's tend to change the *V-3d* filling away from its nominal half-filled value, with the e_g^π orbitals competing with the otherwise dominant a_{1g} orbital. Loss of this near orbital polarization of the a_{1g} orbital is associated with a weakening of electron correlations, especially along the V-V dimerization direction. This removes a charge-density wave (CDW) instability along this direction above a critical doping concentration, which further suppresses the metal-insulator transition. Our study also suggests that the MIT is predominantly driven by a correlation-induced CDW instability along the V-V dimerization direction.

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I. INTRODUCTION

Defects determine and control properties of solids and to a large degree impart specific functionalities to them [1]. Harvesting these functionalities will play a key role in advanced electronic materials for future information technologies, such as neuromorphic [2] and quantum computing [3]. There is a significant gap in our understanding of how defects influence technologically relevant phase transitions, such as the metal-insulator transition (MIT), in strongly correlated materials [4,5]. Closing this gap is particularly challenging when strong nonlocal electron-electron correlation effects are coupled with the strong local interactions of defects with the lattice [6–8]; such a fundamental understanding is necessary for paving the way for robust future technologies based on correlated materials.

VO₂ is formally a $3d^1$ system which is expected to have a metallic ground state owing to its half-filled *d* band. While indeed metallic at high temperatures, the compound is in

a “bad metal” regime because its resistivity is above the Mott-Ioffe-Regel bound [9,10]. Below the transition temperature, $T_{\text{MIT}} \sim 340$ K, VO₂ becomes insulating [11,12]. This electronic transition is accompanied by a structural phase transition, in which the high-temperature and high-symmetry rutile (*R*) phase [Fig. 1(a)] transforms to a low-temperature low-symmetry monoclinic (*M*) phase by the formation of V-V dimers along the rutile *c* axis. As such this MIT is considered a Peierls-Mott type transition [13,14]. It has been a long-standing problem to understand if the MIT is driven primarily by electron correlations [15] or by intrinsic structural instabilities [16], and understanding this is crucial to the control of MIT in correlated solids.

The nominally V⁴⁺ vanadium atoms in the rutile phase sit at the center of distorted oxygen octahedra. This splits the otherwise low-energy triply degenerate t_{2g} manifold of *V-3d* into a single a_{1g} orbital and a doubly degenerate e_g^π combination of orbitals. It is the a_{1g} orbital in the rutile phase that takes part in forming the dimerized singlet state across the MIT, thereby opening up an electronic gap. Indeed, detailed x-ray absorption, x-ray diffraction, and transport studies on thin films across the MIT reveal tunability of T_{MIT} through strain

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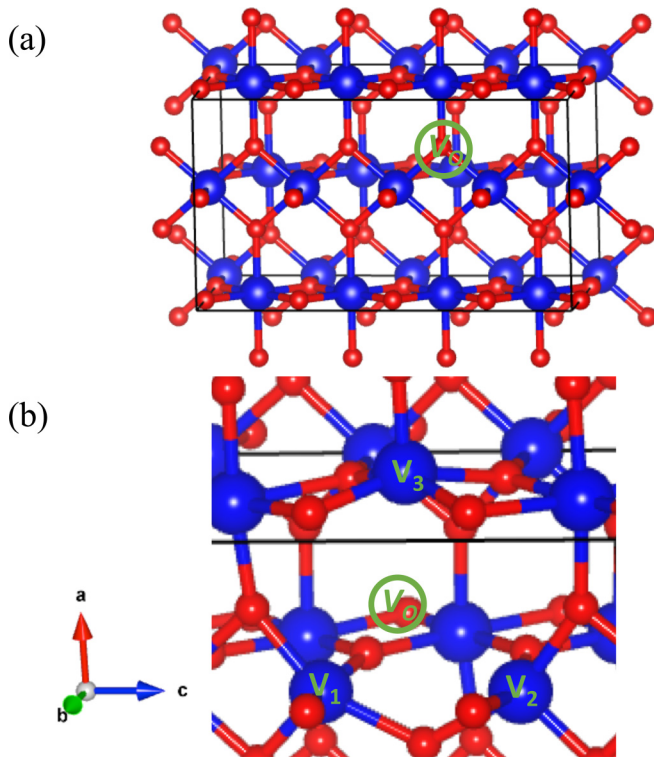


FIG. 1. (a) shows the DFT-SCAN relaxed structure of our 48-atom VO_2 supercell. The V_O site is labeled. (b) shows the strong local distortions seen around the V_O site in relaxed $\text{VO}_{2-\delta}$. The nearest neighbor V atoms to the V_O site are also labeled. [V (blue), O (red)]

or interdiffusion, which appears to correlate with changes in a_{1g} orbital occupancy [15,17,18].

Doping VO_2 with external substitutional dopants such as W in the V site has been shown to tune T_{MIT} , and partially reverts transport back to normal behavior [10]. Doping thin films of metallic R phase VO_2 with intrinsic oxygen vacancies was recently shown to fully suppress the metal to insulator transition with no observed structural transitions down to 50 K [19]. It is not clear what is the underlying mechanism behind the tunability or suppression of the MIT with doping and how this tunability/suppression depends on the doping concentration or the type of dopant. Understanding this can perhaps also reveal what factors are crucial in driving the MIT in the first place in stoichiometric VO_2 .

In this paper, we investigate the influence of doping VO_2 with V_O and both capture and explain the experimentally observed suppression of the Peierls-Mott type MIT. We accomplish this by using density functional theory based methods (DFT and DFT+ U), together with correlated-electronic structure methods, such as dynamical mean-field theory (DMFT) [20] and quantum Monte Carlo (QMC) [21]. QMC is a very accurate ground state correlated method which gives accurate vacancy formation energies and electron densities. The use of DMFT allows us to expand the investigation into excited state spectra. We obtain critical insights on what factors are crucial in driving and controlling the MIT in VO_2 , which should be relevant for similar bad-metal systems [22–24]. We also assess the importance of including electronic correlations in describing the physics of doping with defects and elucidate

the link between correlations and orbital filling. We conclude that electronic interactions are the primary driver of the MIT, and the structural distortion is a secondary consequence.

II. METHODS

We perform electronic-structure calculations using a series of complementary methodologies that allow us to capture effects of structural distortions, account for strong electron correlations on the V sites, and access both ground- and excited-state properties, with cross validation of computed quantities whenever possible. The following subsections detail the different methodologies we have employed.

A. Density functional theory (DFT)

Atomic structures were relaxed using atomic forces obtained from non-spin-polarized density functional theory (DFT) based calculations with the SCAN meta-generalized-gradient (meta-GGA) functional [25,26] as well as the Perdew, Burke, and Ernzerhof (PBE) functional with a Hubbard ‘ U ,’ i.e., PBE+ U , with $U = 4$ eV in the rotationally invariant Dudarev [27] approach, as implemented in the VASP package [28] using PAW pseudopotentials [29]. All calculations were performed in a 48-atom supercell with dimensions: $L_x = L_y = 6.4412$ Å and $L_z = 11.4112$ Å, along the orthogonal **a**, **b**, **c** directions as shown in Fig. 1(a) in the main text. Atomic relaxations were performed using a $4 \times 4 \times 4$ **k** mesh to perform the Brillouin-zone integration with a gaussian smearing of 0.2 and a plane-wave kinetic-energy cutoff of 400 eV, using the ‘accurate’ setting for the precision tag in VASP. The ‘V’ and ‘O’ PAW potentials had 13 and 6 valence electrons, respectively. Forces were converged down to 0.01 eV/Å. The supercell oxygen vacancy structures were obtained by removing one oxygen atom from the 48-atom supercell (corresponding to $\text{VO}_{2-\delta}$ with $\delta = 0.0625$). The SCAN and PBE+ U total density of states (DOS) for pure and nonstoichiometric VO_2 are shown in the Appendix figures 8 and 9.

B. Quantum Monte Carlo (QMC)

The diffusion Monte Carlo (DMC) flavor of continuum quantum Monte Carlo methods was performed on the same structure using QMCPACK [30]. Diffusion Monte Carlo is a highly accurate wave-function based projector method that improves variationally as the starting, or trial, wave function is improved. An accurate trial wave function is essential to minimize residual fixed node/phase error in the method. The basic form of the trial wave function used here is a product of an up/down spin factorized Slater determinant and a Jastrow correlation factor, as follows:

$$\Psi_T(R) = e^{J(R)} D^\uparrow(R^\uparrow) D^\downarrow(R^\downarrow). \quad (1)$$

The nodal/phase structure of the trial wave function is determined by the single particle orbitals populating the determinants. Trial orbitals were obtained within LSDA+ U via the QUANTUM ESPRESSO code for all atomic structures. The U value was selected to be 3.5 eV since this value minimizes the variational DMC total energy for VO_2 as demonstrated by prior studies [6,31]. A ferromagnetic configuration was

chosen for the V sites since this arrangement of magnetic moments is more robust to changes in the lattice induced by defects. Since the spin gap in the materials is small, this choice has a negligible impact on the resulting defect formation energies. The trial Jastrow factor was represented as a sum of one- and two-body correlation factors represented in a B-spline basis along electron-electron or electron-ion pair distances. The Jastrow factor was variationally optimized with respect to the total energy using the linearized optimization method. The bulk optimized Jastrow factor was used in both bulk and defective phases to minimize the potential impact of pseudopotential locality errors in the subsequent DMC calculations, similar to what is commonly done for van der Waals systems. In both the bulk and defective cases, the absolute variance to energy ratio resulting from the Jastrow was near 0.026 Ha, indicating uniform quality across the structures. Diffusion Monte Carlo total energies and spin densities were obtained by averaging over a $2 \times 2 \times 2$ supercell twist grid. DMC runs at each twist were performed with a large population of random walkers ($\approx 14\,000$ walkers per twist) and a small timestep of 0.005 Ha^{-1} resulting in an acceptance ratio of 99.6%. Validated [31–33] norm-conserving RRKJ pseudopotentials were used for vanadium (Ne core) and oxygen (He core). The T -move scheme was used to maintain the variational principle in DMC calculations involving these nonlocal pseudopotentials. All QMC related simulation workflows were driven with the Nexus [34] workflow automation system.

Optical gaps were calculated for $M_1 \text{VO}_2$ cells [structure shown in Fig. 5(a)] containing a single oxygen vacancy in the following manner. A single oxygen vacancy was introduced into a 48 atom VO_2 cell in M_1 phase at each of two inequivalent sites—O(I) and O(II). The atomic structures were then relaxed via DFT using the SCAN functional. A $4 \times 4 \times 4$ set of supercell twist angles was considered for the search space for minimum band gap. At each twist the direct gap from LDA+ U was used as a proxy to select twist angles with the greatest likelihood of having a minimum gap. Twist angles with minimum LDA+ U direct gap in either spin channels were considered for subsequent DMC optical gap calculations. A selection was made both among twist angles that preserved supercell charge neutrality as well among those that admitted a net supercell charge. This was done for both inequivalent oxygen vacancy sites, resulting in two candidate supercell twist angles for each of the two vacancy structures. The direct gap within each cell consistent with the twisted boundary conditions was then calculated within DMC for each spin channel, by promoting one electron from the highest occupied state to the lowest unoccupied one according to the LDA+ U Kohn-Sham eigenvalues, as is standardly done. Gaps obtained in this way represent upper bounds to the minimum possible gap that would result from an exhaustive search over all supercell twists.

Since the oxygen dimer formation energy has different amounts of error in the different methods used, we calculate the oxygen vacancy formation energy in VO_2 using atomic oxygen and bulk VO_2 as a reference using this formula:

$$E_f[\text{V}_O] = E_{\text{total}}[n(\text{VO}_{2-\delta})] - E_{\text{total}}[n(\text{VO}_2)] - E[\text{O}] \quad (2)$$

where the total energies are calculated at 0 K and $n = 16$ is the number of formula units in our 48-atom supercell, and $\delta = 0.0625$. $E[\text{O}]$ is taken to be one half the total energy of an oxygen dimer.

C. Dynamical mean field theory (DMFT)

Calculations beyond DFT are put into practice to account for strong electron correlations on the V sites. We use a charge self-consistent DFT+dynamical mean-field theory (DMFT) framework [35], building up on a mixed-basis pseudopotential approach for the DFT part and the continuous-time quantum-Monte-Carlo method, as implemented in the TRIQS package [36,37], for the DMFT impurity problem. The GGA in the PBE-functional form is employed within the Kohn-Sham cycle. Vanadium $3d4s4p$ and oxygen $2s2p$ were treated as valence electrons in the pseudopotential generation scheme. Locally, threefold effective V($3d$) Wannier-like functions define the correlated subspace, which as a whole consists of the corresponding sum over the various V sites in the defect problem. Projected-local orbitals [38] of $3d$ character provide the effective functions from acting on Kohn-Sham conduction states above the O($2p$)-dominated band manifold. The selected threefold functions are given by the local three-orbital sector lowest in energy, respectively. Each V site marks an impurity problem, and the number of symmetry-inequivalent vanadium sites provides the number of single-site DMFT problems to solve. A three-orbital Hubbard Hamiltonian of Slater-Kanamori form, parametrized by the Hubbard $U = 4 \text{ eV}$ and the Hund's exchange $J_H = 0.7 \text{ eV}$, acts on each V site. These values for the local Coulomb interactions are close to an effective $U_{\text{eff}} = U - J = 3.5 \text{ eV}$, which was shown to be optimal in previous studies on VO_2 [6,31]. A double-counting correction of the fully-localized form [39] is utilized. The analytical continuation of the finite-temperature Green's functions on the Matsubara axis $i\omega$ to real frequencies is performed via the maximum-entropy method as well as with the Padé scheme.

Atomic structures were relaxed using atomic forces obtained from DFT based calculations with the SCAN functional [25,26]. All calculations were performed in a 48-atom supercell as shown in Fig. 1(a). Oxygen vacancy structures were obtained by removing one oxygen atom from the 48-atom supercell (i.e., one missing oxygen in a 16 f.u. VO_2 supercell corresponding to $\text{VO}_{2-\delta}$ with $\delta = 1/16 = 0.0625$). Relaxed structure [shown in Fig. 1(b)] suggests a significant degree of local distortion around the V_O site. It is not immediately clear how important are these distortions in describing the observed suppression of MIT. To assess this, we also perform calculations using a virtual crystal approximation (VCA) method whereby electrons are added to VO_2 to mimic electronic doping, without any atomic relaxation/distortion. VCA is site/chemical selective. In more detail, an oxygenlike pseudoatom of charge $Z = 8 + \delta$, i.e., a nominal mixture of an O and an F atom, is utilized within VCA to mimic the appearance of oxygen vacancies. Calculations beyond DFT, such as a charge self-consistent DFT+DMFT method [35–37] employed in a real-space formulation to treat several-coupled impurity problems as well as the diffusion Monte Carlo (DMC) flavor of continuum QMC method using QMCPACK

[6,30,31], are put into practice to account for strong electronic correlations on the V sites. Oxygen vacancy formation energy was calculated using Eq. (2).

III. RESULTS AND DISCUSSION

The V_O formation energies obtained from DMFT and QMC calculations are 5.09 and 5.10(1) eV, respectively, in excellent agreement with each other. As such both of these strongly-correlated techniques must capture the changes in the underlying electronic structure due to V_O 's appreciably well, in turn implying a coupling of V_O 's to the strength of electron correlations. The charge density difference compared to stoichiometric VO_2 from DMFT and DMC results are shown in Figs. 2(a) and 2(b), respectively. While absolute values are not identical, possibly due to different types of pseudopotentials (see Methods), at both levels of theory, the largest change in charge density appears to be around the three vanadium atoms closest to the V_O as shown in Fig. 1(b). Specifically, QMC charge densities show that the three underbonded $V_{1,2,3}$ atoms have an excess of electrons compared to pristine VO_2 (a cutoff distance of 1.26 Å was used for charge integration). A local perturbation of the charge density in the presence of V_O , as

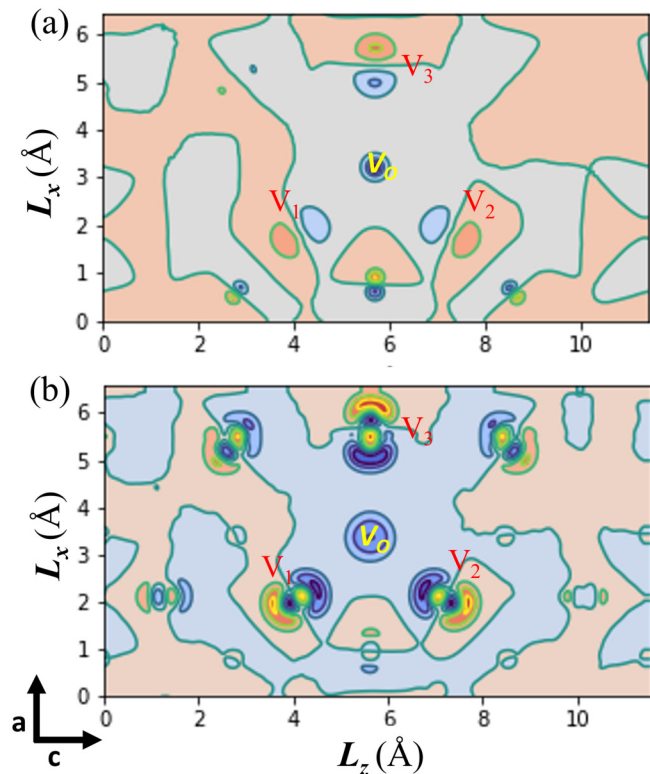


FIG. 2. Contour plots of charge-density difference (units of $e/(\text{a.u.})^3$) between nonstoichiometric and stoichiometric VO_2 in the central plane containing the V_O from (a) DMFT and (b) QMC calculations. Both levels of theory suggest that electronic reorganization propagates from local changes around the defect site. The three V-atoms closest to the V_O site [labeled in Fig. 1(b)], show the largest density changes. (blue/red show density loss/gain compared to pristine VO_2 . The color-bar ranges from $\{-4, 3\}$ and $\{-1.2, 1.2\}$ for DMFT and QMC plots, respectively.)

opposed to complete delocalization of the excess electrons from V_O as one might expect in a regular metal, could be reminiscent of its bad-metal behavior. Also, the agreement between DMFT and DMC on ground-state properties such as vacancy formation energy and charge density gives greater confidence in the DMFT excited-state properties, such as the spectral function.

Figure 3(a) shows the orbitally-resolved local spectral function $A(\omega)$ of $V-3d^1$ for stoichiometric R -phase VO_2 obtained at a temperature of $T = 370$ K, well above $T_{MIT} = 340$ K. In addition to a narrow quasiparticle peak close to $\omega = 0$, a lower Hubbard peak is seen at ~ 1.35 eV below the Fermi level. This is in contrast to the density of states obtained from DFT-based methods (see Appendix) but in good agreement with the photoelectron spectroscopy (PES) results [12] that show a small low-energy bump in the valence spectrum of VO_2 around ~ 1 eV. We find these states to be dominated by a_{1g} orbital contributions compared to the two degenerate e_g^π orbitals (only the average e_g^π contribution is shown). The same PES experiment [12] shows these localized $V-3d^1$ states to be occupied even in the insulating M phase, but they are now part of the doubly-occupied V-V dimerized singlet state, which is also composed of the a_{1g} orbitals. Therefore one might expect that disrupting this near orbital polarization of a_{1g} orbitals should have an influence on the MIT in VO_2 . Indeed, x-ray dichroism experiments [17] showed that lowering orbital polarization of a_{1g} via strain led to a reduced T_{MIT} . We now explore the influence of V_O 's on orbital occupancies and the resultant orbital dichroism, defined as $D_{orb} = (n_{a_{1g}} - n_{e_g^\pi}) / (n_{a_{1g}} + n_{e_g^\pi})$, where n_α is the electron density from the orbital α , which loosely corresponds to the measured quantity in x-ray dichroism experiments [15,17].

The orbitally-resolved spectral function from DMFT for $VO_{2-\delta}$ [Fig. 3(b)] is very different from that of VO_2 . Clearly, the low-energy bump at ~ 1.35 eV has a much-reduced intensity, and the width of the quasiparticle peak has significantly widened, leading to its reduced peak height—suggesting weakened electron-electron correlations. In particular, the e_g^π orbital occupancy appears to be competing with the a_{1g} occupancy, indicating that the near orbital a_{1g} polarization seen in VO_2 is now reduced. The integrated V- d charge is now $1.12e^-$, much different from the nominal $1e^-$ in stoichiometric VO_2 and consistent with the QMC charge density analysis discussed above. This strongly indicates that in the presence of V_O , reduction of the near orbital polarization of the a_{1g} orbital and concomitant weakening of electronic correlations lead to suppression of the MIT.

In order to investigate the importance of capturing the large local distortion seen in our DFT-relaxed structure [Fig. 1(b)], we performed DMFT calculations in the VO_2 unit cell using a virtual-crystal approximation (VCA). This results in a 1.12 electron filling of the V site in the converged DFT+DMFT calculation. The difference plot of the quasiparticle dispersion as shown in Fig. 4(c) is consistent with this electron doping. In addition, loss of \mathbf{k} -resolved spectral-weight intensity at low energy is in line with the larger overall quasiparticle weight in the defective case. This suggests that while details of the distortion are necessarily important in getting the correct vacancy-formation energetics as well as correlating local bond disproportionation around the defect to charge reorganization

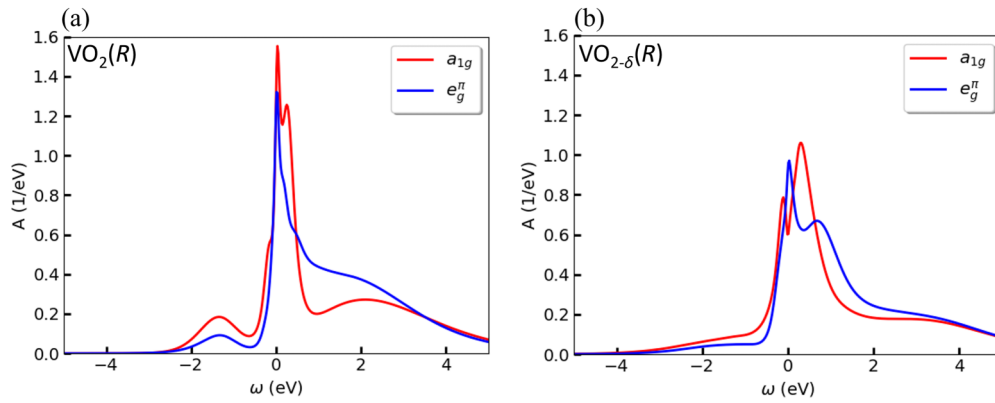


FIG. 3. (a) and (b) show the orbitaly-resolved local $V-t_{2g}$ spectral functions $A(\omega)$ obtained from real-space DFT+DMFT supercell calculations for pristine (VO_2) and nonstoichiometric ($\text{VO}_{2-\delta}$) R phase, respectively. In the pristine case, a lower Hubbard peak at ~ 1.35 eV is seen that is predominantly of a_{1g} type, indicative of strong electronic correlations. Introducing V_O 's suppresses both the quasiparticle peak at low energy as well as the Hubbard peak.

to obtain the correct orbital weights, qualitative changes in the relative orbital occupancies with doping should be captured even in the absence of such localized distortions.

Optical gaps were calculated for M_1 VO_2 cells containing a single oxygen vacancy using DMC (details in Methods section). At each twist the direct gap from LDA+ U was used as a proxy to select twist angles with the greatest likelihood of

having a minimum gap. QMC estimations of the optical band gap in a 48-atom supercell of the insulating M_1 phase showed a reduction in the gap from 0.8(1) eV in bulk [21] to 0.48(6) or 0.00(6) eV depending on which oxygen site the vacancy was created. Closing of the gap in the M_1 phase even with the presence of a single vacancy suggests that the insulating state is at the verge of an electronic instability. Charge-density

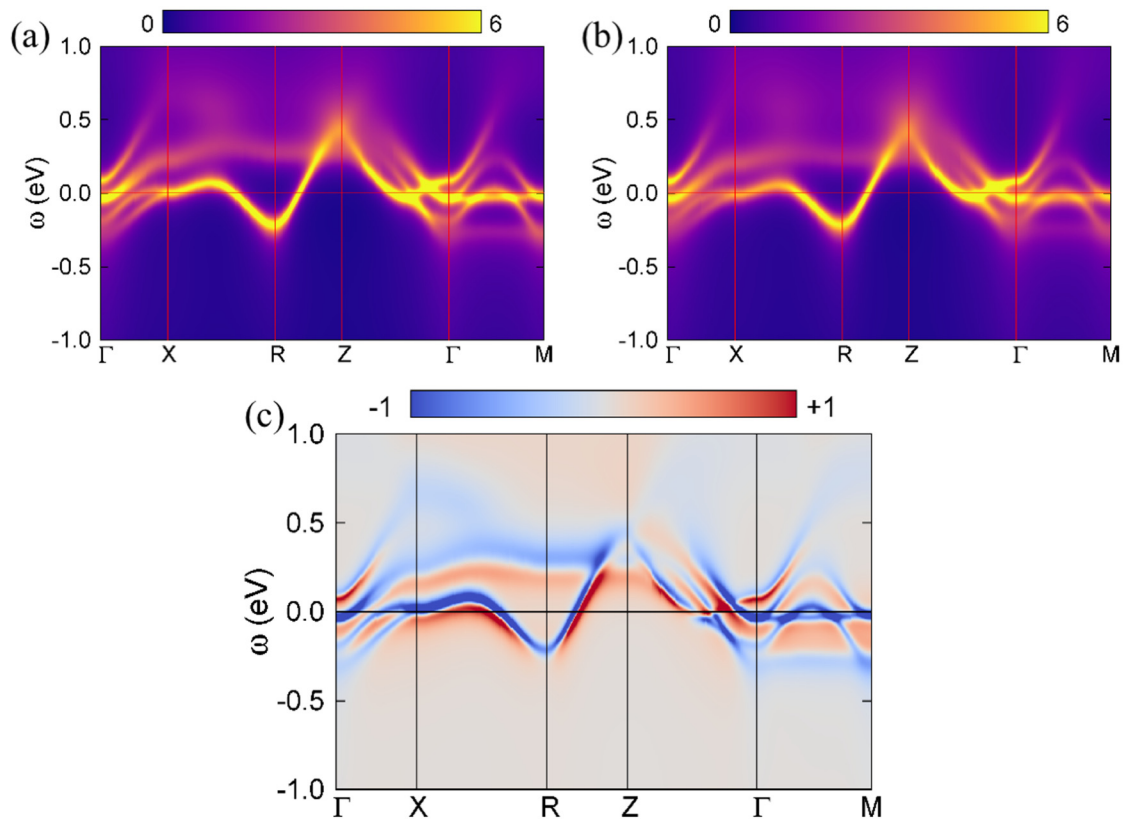


FIG. 4. (a) and (b) show the \mathbf{k} -resolved spectral function of pristine VO_2 and $\text{VO}_{2-\delta}$ (within VCA) for $\delta \sim 0.06 e^-$, respectively, from our DMFT calculations at $T \sim 370$ K. (c) shows the difference of the \mathbf{k} -resolved spectral function between defective and pristine VO_2 within VCA, for a charge doping of $0.06 e^-$. Significant reorganization of spectral weights is observed, with a stronger reduction around $\omega = 0$.

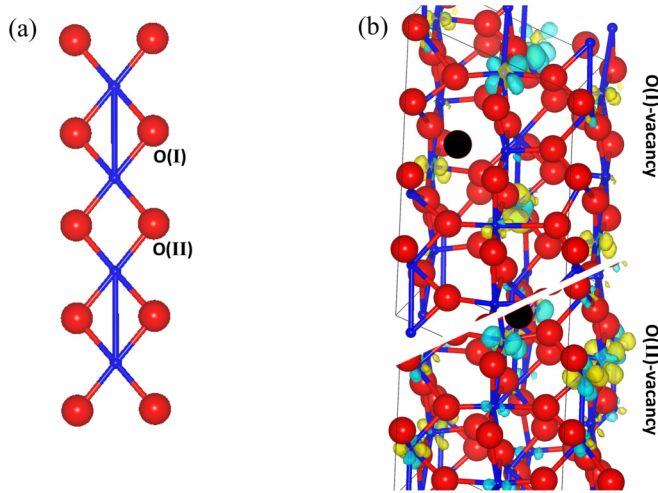


FIG. 5. (a) Fragment of the atomic structure of the M_1 phase of VO_2 showing the 1D V-V dimerized chain and the two inequivalent oxygen sites. (b) shows the charge-density differences corresponding to the lowest optical excitation for the two oxygen vacancies in the M_1 phase. [O (red sphere), V (blue sphere), O_v (black sphere), V-V dimer (blue bonds), isosurface value = $1.1\text{E-}4e^-/\text{\AA}^3$ with $+/-$ = yellow/green]

differences corresponding to the lowest optical excitations for the two oxygen vacancy positions in the M_1 phase, as shown in Fig. 5(b), suggest that they are $d-d$ -type excitations, specifically between d orbitals in-plane (a_{1g}) and out-of-plane (e_g^π 's) containing V-V dimers. Persistence of such gapless $d-d$ -type excitations therefore indicates the absence of the near orbital polarization of a_{1g} orbitals, consistent with the earlier DMFT results. Suppression of the MIT in nonstoichiometric VO_2 is consistent with recent experiments where the metallic R phase was seen to be stable even down to 50 K [19]. Since this behavior is experimentally similar to W -doped VO_2 , it appears that introducing V_O in VO_2 is similar to electronically doping it, even in the metallic phase, as confirmed by DMFT. Given that the changes are local, as inferred from our charge-density plots (Fig. 2), our calculations suggest that there is some kind of a percolation threshold that needs to be exceeded in order to suppress the MIT. This hypothesis is in agreement with experimental observations [19] which estimate a critical doping concentration of $\delta_c^{\text{exp}} = 0.098$ to be necessary to fully suppress the metal-insulator transition.

To see the presence of such a critical concentration, and its relationship as well as manifestation in terms of the suppression of the near orbital polarization, we estimate D_{orb} as defined above from VCA calculations performed at a series of doping concentrations (δ) as shown in Fig. 6. D_{orb} becomes initially more positive with δ but quickly reduces in magnitude, consistent with the expected relative loss of the a_{1g} orbital weights. Above $\delta = \delta_c \sim 0.07$, D_{orb} falls below its pristine VO_2 value, indicative of a critical concentration above which no MIT can be realized. This observation proves the direct link between suppression of near-orbital polarization of a_{1g} and the suppression of the MIT. Given that D_{orb} can be loosely connected to the experimentally measured x-ray

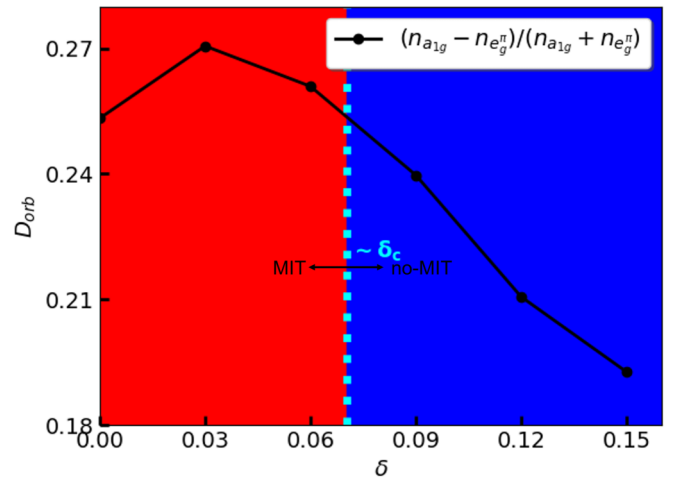


FIG. 6. (a) Orbital-dichroism (D_{orb}) from DMFT-VCA calculations shows that with electron doping the dichroism initially increases but subsequently becomes less positive with a diminished magnitude. At $\delta_c \sim 0.07$ its value dips below that of pristine VO_2 and is indicative of a doping level beyond which MIT would be suppressed. This value is close to the experimental estimation of $\delta_c^{\text{exp}} = 0.098$ in VO_2 thin films.

dichroism [17], our results suggest that the physics underlying MIT suppression and the tuning of T_{MIT} in VO_2 by means of V_O 's, extrinsic-dopants, strain, or electric fields is very similar, and all of these approaches are different controls to modify the a_{1g} 's relative occupancy and reduce electron-electron correlations to influence the MIT. X-ray dichroism studies in well-controlled nonstoichiometric VO_2 thin films should experimentally confirm this claim.

Electron-electron correlations are thought to be important for describing the bad-metal behavior of VO_2 as well as causing V-V dimerization in the M phase [14,15]. A 1D Peierls instability could be driven by a 1D charge-density wave (CDW) instability, which would correspond to a nesting vector at $k \sim 2k_F$, where k_F is the Fermi wave vector. If this is indeed the case, it will show up as a 'bump' in the momentum distribution $n(k)$. When using a value of ' U ' optimized by DMC, the $n(k)$ from LSDA+ U and DMC have negligible differences for $k > k_F$ [40], as such we study $n(k)$ using LSDA+ U . Indeed, the $n(k)$ obtained from our LSDA+ U calculation for the R -phase VO_2 shows such a bump at $\sim 2k_F = 2.49$ a.u., where the k vector is plotted conjugate to the c direction as shown in Fig. 7 and recently published by some of us in Ref. [40]. No such oscillatory features are observed along the other k directions. This shows the presence of a 1-D CDW instability with a nesting vector of $2k_F$, which would be required to drive the V-V dimerization, resulting in the insulating M phase. The bump is also expected to cause divergences in the response functions, such as the Lindhard susceptibility, and thereby lead to its bad-metal behavior—i.e. the violation of the Wiedemann-Franz law [10].

In the presence of V_O , this bump at $\sim 2k_F$ vanishes (Fig. 7), altering the bad-metal characteristics of VO_2 , and the density monotonically decreases with increasing momentum. This would result in divergenceless response functions, and thereby

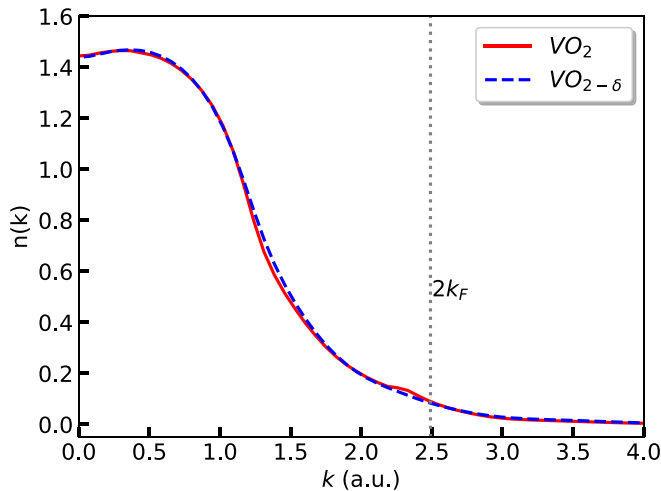


FIG. 7. Momentum density along k direction conjugate to the V-V dimerization direction for pristine and nonstoichiometric VO_2 from LSDA+ U calculations. Vanishing of the $\sim 2k_F$ peak in $\text{VO}_{2-\delta}$ suggests a lack of a charge-density wave (CDW) when V_O 's are introduced, thereby altering its bad-metal behavior.

a lack of an electronic instability to drive a phase transition. This is a consequence of the weakening of electron-electron correlation, as also suggested from our DMFT results, whereby the filling is not $1e^-$ on each V site and the near orbital polarization of a_{1g} is lacking. Suppressing this electronic driving force for a Peierls distortion should also result in suppression of the structural transition to the M phase.

IV. CONCLUSION

Oxygen vacancies donate electrons, and the resulting orbital-dependent charge-doping reduces the near orbital polarization of the a_{1g} orbitals seen in R-phase VO_2 . This reduction is associated with a weakening of the electronic correlations and leads to a reduced drive for V-V dimerization. This not only suppresses the MIT but also substantially alters the “bad metal” characteristics of the metallic phase in nonstoichiometric VO_2 . Our study reaffirms the intricate connection between structural dimerization and electron-correlation in VO_2 and suggests that the MIT is predominantly driven by a correlation-induced electronic instability and not a struc-

tural instability, with the a_{1g} occupancy being the primary knob to control the MIT via different external perturbations such as V_O 's, extrinsic dopants, strain, or electric fields. This understanding of the presence of a single fundamental knob that allows control over complex coupled phase transitions in correlated solids can be relevant to engineering functional interfaces of correlated oxides and also aid in understanding technologically relevant MIT systems that show concomitant magnetic and/or structural transitions, such as manganites [22] and the family of nonstoichiometric ABO_{3-x} compounds [23].

In addition, simulation inputs, and outputs for QMC, DMFT and DFT calculations performed in this work are available via the Materials Data Facility [41].

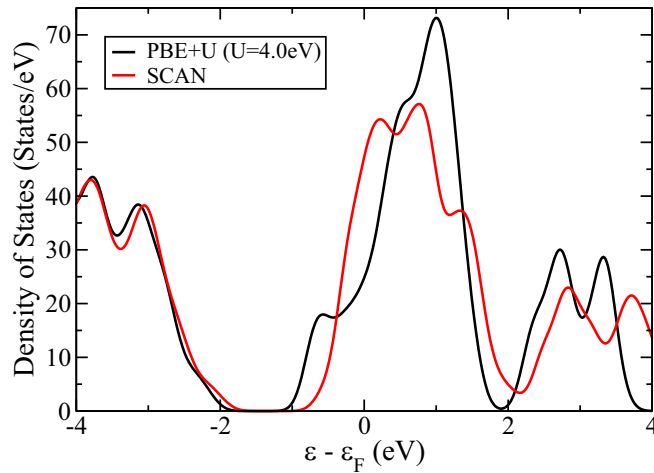
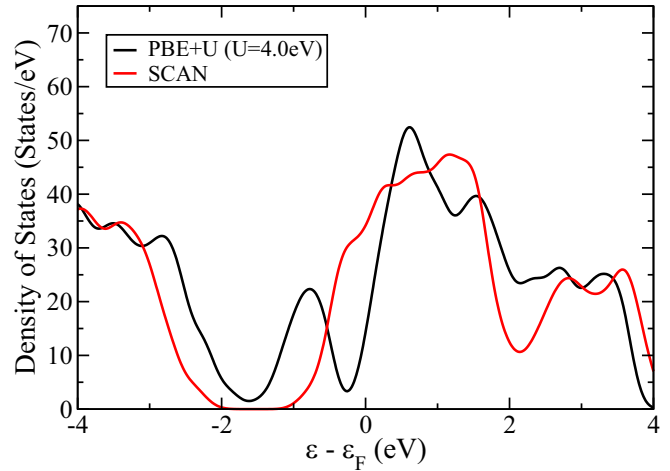
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APPENDIX

See Figs. 8 and 9.

FIG. 8. Total density of states for VO₂ from SCAN and PBE+U calculations.FIG. 9. Total density of states for nonstoichiometric VO₂ from SCAN and PBE+U calculations.

- [1] C. Freysoldt, B. Grabowski, T. Hickel, J. Neugebauer, G. Kresse, A. Janotti, and C. G. Van de Walle, *Rev. Mod. Phys.* **86**, 253 (2014).
- [2] D. B. Strukov, G. S. Snider, D. R. Stewart, and R. S. Williams, *Nature (London)* **453**, 80 (2008).
- [3] J. R. Weber, W. F. Koehl, J. B. Varley, A. Janotti, B. B. Buckley, C. G. Van de Walle, and D. D. Awschalom, *Proc. Natl. Acad. Sci.* **107**, 8513 (2010).
- [4] I. H. Inoue and M. J. Rozenberg, *Adv. Funct. Mater.* **18**, 2289 (2008).
- [5] N. Shukla, A. V. Thathachary, A. Agrawal, H. Paik, A. Aziz, D. G. Schlom, S. K. Gupta, R. Engel-Herbert, and S. Datta, *Nat. Commun.* **6**, 7812 (2015).
- [6] Y. Sharma, J. Balachandran, C. Sohn, J. T. Krogel, P. Ganesh, L. Collins, A. V. Ievlev, Q. Li, X. Gao, N. Balke, O. S. Ovchinnikova, S. V. Kalinin, O. Heinonen, and H. N. Lee, *ACS Nano* **12**, 7159 (2018).
- [7] J. Ding, J. Balachandran, X. Sang, W. Guo, J. S. Anchell, G. M. Veith, C. A. Bridges, Y. Cheng, C. M. Rouleau, J. D. Poplawsky, N. Bassiri-Gharb, R. R. Unocic, and P. Ganesh, *Chem. Mater.* **30**, 4919 (2018).
- [8] A. Zylbersztejn and N. F. Mott, *Phys. Rev. B* **11**, 4383 (1975).
- [9] V. J. Emery and S. A. Kivelson, *Phys. Rev. Lett.* **74**, 3253 (1995).
- [10] S. Lee, K. Hippalgaonkar, F. Yang, J. Hong, C. Ko, J. Suh, K. Liu, K. Wang, J. J. Urban, X. Zhang, C. Dames, S. A. Hartnoll, O. Delaire, and J. Wu, *Science* **355**, 371 (2017).
- [11] J. B. Goodenough, *J. Solid State Chem.* **3**, 490 (1971).
- [12] C. Blaauw, F. Leenhouts, F. van der Woude, and G. A. Sawatzky, *J. Phys. C: Solid State Phys.* **8**, 459 (1975).
- [13] S. Biermann, A. Poteryaev, A. I. Lichtenstein, and A. Georges, *Phys. Rev. Lett.* **94**, 026404 (2005).
- [14] W. H. Brito, M. C. O. Aguiar, K. Haule, and G. Kotliar, *Phys. Rev. Lett.* **117**, 056402 (2016).
- [15] A. X. Gray, J. Jeong, N. P. Aetukuri, P. Granitzka, Z. Chen, R. Kukreja, D. Higley, T. Chase, A. H. Reid, H. Ohldag, M. A. Marcus, A. Scholl, A. T. Young, A. Doran, C. A. Jenkins, P. Shafer, E. Arenholz, M. G. Samant, S. S. P. Parkin, and H. A. Dürr, *Phys. Rev. Lett.* **116**, 116403 (2016).
- [16] J. D. Budai, J. Hong, M. E. Manley, E. D. Specht, C. W. Li, J. Z. Tischler, D. L. Abernathy, A. H. Said, B. M. Leu, L. A. Boatner, R. J. McQueeney, and O. Delaire, *Nature (London)* **515**, 535 (2014).
- [17] N. B. Aetukuri, A. X. Gray, M. Drouard, M. Cossale, L. Gao, A. H. Reid, R. Kukreja, H. Ohldag, C. A. Jenkins, E. Arenholz, K. P. Roche, H. A. Dürr, M. G. Samant, and S. S. P. Parkin, *Nat. Phys.* **9**, 661 (2013).
- [18] N. F. Quackenbush, H. Paik, M. E. Holtz, M. J. Wahila, J. A. Moyer, S. Barthel, T. O. Wehling, D. A. Arena, J. C. Woicik, D. A. Muller, D. G. Schlom, and L. F. J. Piper, *Phys. Rev. B* **96**, 081103(R) (2017).
- [19] Z. Zhang, F. Zuo, C. Wan, A. Dutta, J. Kim, J. Rensberg, R. Nawrodt, H. H. Park, T. J. Larrabee, X. Guan, Y. Zhou, S. M. Prokes, C. Ronning, V. M. Shalaev, A. Boltasseva, M. A. Kats, and S. Ramanathan, *Phys. Rev. Appl.* **7**, 034008 (2017).
- [20] F. Lechermann, W. Heckel, O. Kristanovski, and S. Müller, *Phys. Rev. B* **95**, 195159 (2017).
- [21] H. Zheng and L. K. Wagner, *Phys. Rev. Lett.* **114**, 176401 (2015).
- [22] I. Loa, P. Adler, A. Grzechnik, K. Syassen, U. Schwarz, M. Hanfland, G. K. Rozenberg, P. Gorodetsky, and M. P. Pasternak, *Phys. Rev. Lett.* **87**, 125501 (2001).
- [23] B. Cui, P. Werner, T. Ma, X. Zhong, Z. Wang, J. M. Taylor, Y. Zhuang, and S. S. P. Parkin, *Nat. Commun.* **9**, 3055 (2018).

- [24] J. Vučičević, D. Tanasković, M. J. Rozenberg, and V. Dobrosavljević, *Phys. Rev. Lett.* **114**, 246402 (2015).
- [25] J. Sun, A. Ruzsinszky, and J. P. Perdew, *Phys. Rev. Lett.* **115**, 036402 (2015).
- [26] J. Sun, R. C. Remsing, Y. Zhang, Z. Sun, A. Ruzsinszky, H. Peng, Z. Yang, A. Paul, U. Waghmare, X. Wu, M. L. Klein, and J. P. Perdew, *Nat. Chem.* **8**, 831 (2016).
- [27] S. L. Dudarev, G. A. Botton, S. Y. Savrasov, C. J. Humphreys, and A. P. Sutton, *Phys. Rev. B* **57**, 1505 (1998).
- [28] G. Kresse and J. Furthmüller, *Phys. Rev. B* **54**, 11169 (1996).
- [29] G. Kresse and D. Joubert, *Phys. Rev. B* **59**, 1758 (1999).
- [30] J. Kim, A. T. Baczewski, T. D. Beaudet, A. Benali, M. C. Bennett, M. A. Berrill, N. S. Blunt, E. J. L. Borda, M. Casula, D. M. Ceperley, S. Chiesa, B. K. Clark, R. C. C. III, K. T. Delaney, M. Dewing, K. P. Esler, H. Hao, O. Heinonen, P. R. C. Kent, J. T. Krogel, I. Kylänpää, Y. W. Li, M. G. Lopez, Y. Luo, F. D. Malone, R. M. Martin, A. Mathuriya, J. McMinis, C. A. Melton, L. Mitas, M. A. Morales, Eric Neuscamman, W. D. Parker, S. D. P. Flores, N. A. Romero, B. M. Rubenstein, J. A. R. Shea, H. Shin, L. Shulenburger, A. F. Tillack, J. P. Townsend, N. M. Tubman, B. V. D. Goetz, J. E. Vincent, D. C. Yang, Y. Yang, S. Zhang, and L. Zhao, *J. Phys.: Condens. Matter* **30**, 195901 (2018).
- [31] I. Kylänpää, J. Balachandran, P. Ganesh, O. Heinonen, P. R. C. Kent, and J. T. Krogel, *Phys. Rev. Mater.* **1**, 065408 (2017).
- [32] J. T. Krogel, J. A. Santana, and F. A. Reboredo, *Phys. Rev. B* **93**, 075143 (2016).
- [33] A. L. Dzubak, J. T. Krogel, and F. A. Reboredo, *J. Chem. Phys.* **147**, 024102 (2017).
- [34] J. T. Krogel, *Comput. Phys. Commun.* **198**, 154 (2016).
- [35] D. Grieger, C. Piefke, O. E. Peil, and F. Lechermann, *Phys. Rev. B* **86**, 155121 (2012).
- [36] O. Parcollet, M. Ferrero, T. Ayril, H. Hafermann, I. Krivenko, L. Messio, and P. Seth, *Comput. Phys. Commun.* **196**, 398 (2015).
- [37] P. Seth, I. Krivenko, M. Ferrero, and O. Parcollet, *Comput. Phys. Commun.* **200**, 274 (2016).
- [38] B. Amadon, F. Lechermann, A. Georges, F. Jollet, T. O. Wehling, and A. I. Lichtenstein, *Phys. Rev. B* **77**, 205112 (2008).
- [39] V. I. Anisimov, I. V. Solovyev, M. A. Korotin, M. T. Czyżyk, and G. A. Sawatzky, *Phys. Rev. B* **48**, 16929 (1993).
- [40] I. Kylänpää, Y. Luo, O. Heinonen, P. R. C. Kent, and J. T. Krogel, *Phys. Rev. B* **99**, 075154 (2019).
- [41] P. Ganesh, F. Lechermann, I. Kylanpaa, J. T. Krogel, P. R. C. Kent, and O. Heinonen, dataset for “Doping a bad metal: Origin of suppression of the metal-insulator transition in nonstoichiometric VO₂”, doi: 10.18126/nrpj-u7bp.
- [42] <http://energy.gov/downloads/doe-public-access-plan>.