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*Research article*

## Estimation of preconsolidation stress of clays from piezocone by means of high-quality calibration data

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**Abstract:** An extensive database of high-quality piezocone (CPTU) and laboratory oedometer test data on onshore and offshore clays worldwide has been established. The database covers a wide range of index parameters and overconsolidation ratios (*OCR*) in the range 1 to 5. The purpose is to derive general correlations to model preconsolidation stress in clays from CPTU data based on high-quality laboratory data. Several studies have already discussed such correlations for different clay types, where the preconsolidation stress is defined as a function of the cone resistance and/or the pore pressure measured in CPTU tests. Often, these correlations are characterized by high uncertainty, mainly because of the sample quality of the laboratory data. New correlations are proposed based on the new database. These correlations are meant to be used for preliminary assessment of preconsolidation stress in the absence of laboratory data or as a comparison tool when limited test data is available.

**Keywords:** preconsolidation stress; *OCR*; CPTU; correlation; clay

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### 1. Introduction

The preconsolidation stress, or yield stress,  $\sigma'_p$  is a fundamental and one of the most relevant engineering parameters of clays. The preconsolidation stress represents the maximum vertical effective overburden stress that the soil has experienced, and is used to define the stress history of the soil by means of the overconsolidation ratio *OCR* ( $=\sigma'_p/\sigma'_v$ , where  $\sigma'_v$  is the present vertical effective stress). The overconsolidation in the soil is often the result of mechanical unloading (i.e., ice melting

or removal of soil) or cementation of the soil skeleton due to aging phenomena or chemical reactions occurring in the soil under some favorable conditions [1]. Furthermore,  $\sigma'_p$  and  $OCR$  strongly correlate with the undrained shear strength of clays [1–4].

The preconsolidation stress  $\sigma'_p$  is commonly determined from laboratory constant-rate-of-strain (CRS) or incrementally loaded (IL) oedometer tests and is generally affected by the quality of the tested sample [5–8], test procedures and the chosen interpretation method [9]. In-situ tests such as the piezocone test (CPTU) are also used in practice to evaluate  $\sigma'_p$  or  $OCR$ , with the advantage of providing continuous measurements with depth. The CPTU test requires, however, laboratory test results for a proper calibration. In absence of site-specific calibration data,  $\sigma'_p$  and  $OCR$  can be estimated from available correlations. Several authors have discussed the interpretation of  $\sigma'_p$  from piezocone for different soil types and proposed models that correlate  $\sigma'_p$  and  $OCR$  with the CPTU parameters [10–15]. Often, these models are calibrated for a specific soil type [14] or are characterized by high scatter around the observed trends [13]. One of the uncertainties that lies behind the literature correlations is the quality of the samples used to derive them. Sample quality is seldom discussed in these studies.

The scope of this study is to evaluate CPTU-based correlations for  $\sigma'_p$  and  $OCR$  based on high-quality data. To do that, a multivariate database consisting of 249 high-quality clay data points covering onshore and offshore clays worldwide has been established. The database covers a wide range of plasticity, with plasticity index  $I_p$  varying between 16 and 110%, water content  $w$  between 25 and 140% and sensitivity  $S_t$  between 1 and 100, with  $OCR$  values ranging from 1 to 5 (normally to medium over-consolidated clays). Sampling depths range between 1 and 35 m. The existing large CLAY/10/7490 database by Ching and Phoon [16] is used for comparison and validation of the trends observed from the compiled high-quality database.

## 2. Multivariate CLAY/9/249 clay database

The compiled database consists of the following nine dimensionless parameters:

1. Preconsolidation stress  $\sigma'_p/p_a$
2. Total vertical stress  $\sigma_v/p_a$
3. Effective vertical stress  $\sigma'_v/p_a$
4. Corrected cone tip resistance  $q_v/p_a$
5. Pore pressure measured above the cone  $u_2/p_a$
6. Static in situ pore pressure  $u_0/p_a$
7. Plasticity index  $I_p$
8. Natural water content  $w$
9. Sensitivity  $S_t$

where  $p_a$  is the atmospheric pressure ( $p_a \sim 100$  kPa).

The multivariate database contains  $n = 249$  clay data points. Full multivariate data is available for all the parameters, except for  $I_p$  and  $S_t$ . The database is labeled as CLAY/9/249, based on the notation (soil type)/(number of parameters of interest)/(number of data points) proposed by Ching and Phoon [16].

Table 1 shows the basic statistics of the CLAY/9/249 database, while Table 2 summarizes the basic properties of each site considered in this study. The inferred  $\sigma'_p$  values refer to CRS oedometer tests, while  $S_t$  was measured from Fall Cone tests. The  $\sigma'_p$  values in this study can be referred to

as “rapid”  $\sigma'_p$ . Several studies have shown that  $\sigma'_p$  from CRS oedometer tests is much larger than that obtained from conventional IL tests (~15–30% higher) with 24-hour load steps because of the higher strain rate in CRS tests [17].

**Table 1.** Basic statistics of CLAY/9/249 database.

Parameter	$\sigma'_p/p_a$	$\sigma_v/p_a$	$\sigma'_v/p_a$	$q_i/p_a$	$u_2/p_a$	$u_0/p_a$	$I_p$ (%)	$w$ (%)	$S_t$ (-)
$n$	249	249	249	249	249	249	158	249	152
Mean	0.67	1.08	0.42	3.84	2.22	0.66	40.40	81.90	22.30
COV	0.69	0.78	0.77	0.67	0.66	0.81	0.38	0.39	1.20
Min	0.12	0.20	0.06	0.66	0.39	0.10	14.00	25.00	1.10
Max	2.80	5.83	2.30	15.00	9.40	3.53	109.9	179.80	99.40

\*COV = coefficient of variation

**Table 2.** Summary of basic properties of the different sites in CLAY/9/249 database.

Site	$n$	Type	$w$ (%)	$I_p$ (%)	$S_t$ (-)	$OCR$	$\Delta e/e_0$
Barents Sea	36	Offshore	25–48	22–42	1.4–2.7	1.2–4.5	0.006–0.062
Bothkennar	2	Onshore	69–70	42–49	8–10	1.9	0.022–0.023
Egypt, Site 1	10	Offshore	109–161	56–69	2.5–5.2	1.2–1.7	0.019–0.054
Egypt, Site 2	6	Offshore	111–138	62–72	3.3–6.2	1.3–2.1	0.03–0.05
Egypt, Site 3	9	Offshore	80–180	32–57	3.1–6.0	1.2–2.1	0.024–0.06
Finland, Site 1	7	Onshore	63–119	39–59	18.1–21.5	1.2–2.0	0.024–0.059
Finland, Site 2	20	Onshore	56–112	16–36	66–99	1.3–1.8	0.021–0.047
Finland, Site 3	38	Onshore	71–111	21–41	33–72	1.3–2.7	0.02–0.059
Finland, Site 4	18	Onshore	87–118	36–58	16–45	1.4–2.4	0.021–0.065
Gulf of Guineas	20	Offshore	79–147	64–110	n/a	1.4–3.5	0.016–0.055
Indian Coast	15	Offshore	48–126	34–68	1.1–5.5	1.3–2.7	0.008–0.054
Lierstranda, Norway	3	Onshore	33–39	14–19	8–12	1.1–1.9	0.025–0.065
Norwegian Sea	3	Offshore	118–130	38–63	6.5–7.3	1.3–1.4	0.052–0.058
Norwegian trench, Site 1	6	Offshore	27–67	22–41	2.5–6.2	1.6–2.3	0.01–0.047
Norwegian trench, Site 2	22	Offshore	55–84	27–43	3.6–8.0	1.1–2.5	0.016–0.066
Norwegian trench, Site 3	5	Offshore	59–75	34–41	3.6–6.0	1.6–2.6	0.012–0.03
Onsøy, Norway	4	Onshore	43–72	24–44	10–12	1.2–1.6	0.049
Vøring basin, Norway	25	Offshore	42–89	30–48	2.1–5.6	1.1–1.8	0.025–0.068

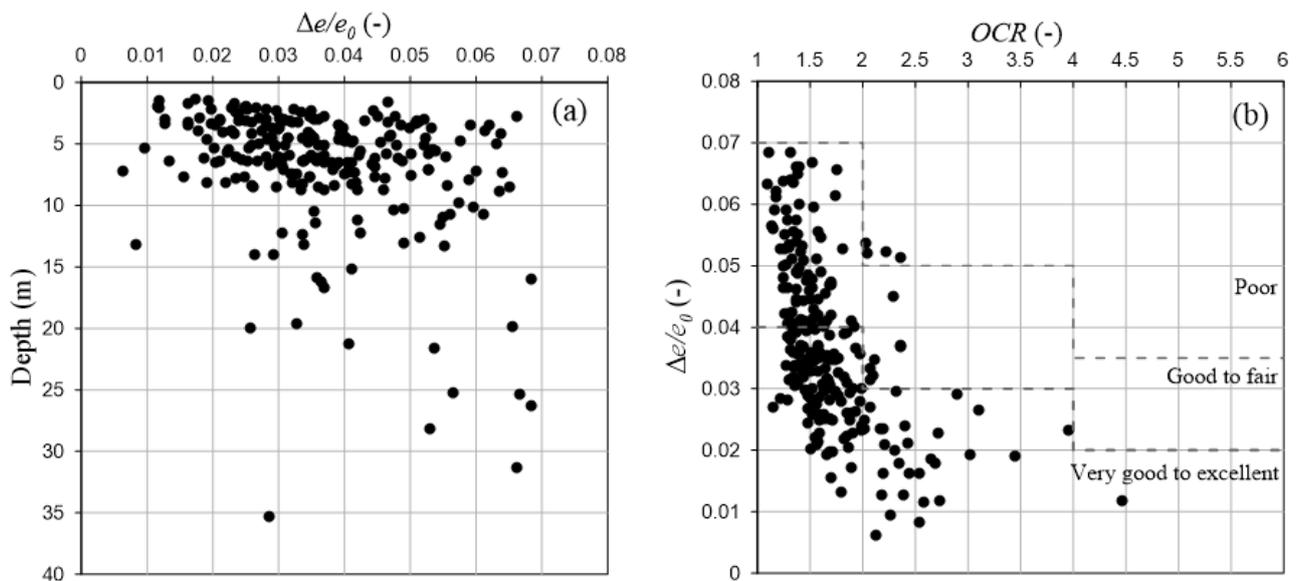
The offshore data and the data for three onshore sites (two in Norway, one in UK) is collected from projects carried out by the Norwegian Geotechnical Institute (NGI). Offshore data is obtained from 75 mm diameter piston sampler, while the 250 mm diameter Sherbrooke block sampler [18] was used at Onsøy, Lierstranda and Bothkennar sites. The NGI data is discussed in Yang et al. [19]. For these data,  $\sigma'_p$  was interpreted according to the method by Casagrande [20].

The majority of the data from Finland is extracted from [7], while additional data was provided by the Laboratory of Earth and Foundation Structures of Tampere University. The Finland data is mainly based on a large 132 mm diameter tube sampler [8]. The interpretation of  $\sigma'_p$  was based on a method that is commonly used in Finland, where the Janbu constrained modulus [21] is fitted to the

CRS stress-strain curve using the least square method for given stress ranges in the pre- and post-yielding regions. The  $\sigma'_p$  is then determined from the intersection of these lines [22]. This gives very consistent  $\sigma'_p$  values for high quality samples of sensitive clays, which would be very close to the ones by Casagrande's method.

Overall, the data contained in the CLAY/9/249 database is to be considered of high-quality, since samples were retrieved using samplers of higher diameter than the standard 50 mm piston or tube sampler. In general, high quality can be expected when using large diameter sampler, provided a favorable geometry of sample tube and cutting shoe [6].

Sample quality was assessed by means of the well-known criterion proposed by Lunne et al. [5]. This criterion considers the volume change during recompression to the in-situ stress ( $\Delta e/e_0$ , where  $e$  is the void ratio) and the  $OCR$ . The range of  $\Delta e/e_0$  values in Table 2 is 0.006–0.068. Figure 1 shows the variation of  $\Delta e/e_0$  with  $OCR$  and depth. In general, there is a tendency of  $\Delta e/e_0$  to increase with depth. According to Figure 1, the data points in the CLAY/9/249 database fall into the "Very good to excellent" and "Good to fair" sample quality categories, except for four data points that lie on boundary between "Good to fair" and "Poor" quality.



**Figure 1.** (a)  $\Delta e/e_0$  versus depth and (b)  $\Delta e/e_0$  versus  $OCR$ .

### 3. Review of existing CPTU-based correlations for $\sigma'_p$ and $OCR$ and comparison with CLAY/9/249 database

Often, engineering properties are derived from normalized CPTU parameters, besides the standard measured parameters. Among these, the most common are:

- Normalized cone resistance  $Q_t = (q_t - \sigma_v)/\sigma'_v$
- Normalized excess pore pressure  $Q_u = (u_2 - u_0)/\sigma'_v$
- Normalized effective cone resistance  $Q_e = (q_t - u_2)/\sigma'_v$
- Pore pressure ratio  $B_q = (u_2 - u_0)/(q_t - \sigma_v)$

In addition,  $(q_t - \sigma_v)$ ,  $(u_2 - u_0)$  and  $(q_t - u_2)$  are commonly referred to as  $q_{net}$ ,  $\Delta u$  and  $q_e$ , respectively.

A number of theoretical and empirical correlations to model  $OCR$  or  $\sigma'_p$  from CPTU parameters have been proposed in the geotechnical literature. These include correlations between  $OCR$  and  $B_q$  [13,23],  $OCR$  and  $Q_t$  [11,24],  $OCR$  and  $Q_u$  [12],  $OCR$  and  $Q_e$  [10,13],  $\sigma'_p$  and  $q_{net}$ ,  $\Delta u$  and  $q_e$  [13,15,25,26].

While the majority of the studies in the literature attempted to empirically correlate  $\sigma'_p$  and  $OCR$  to piezocone parameters, some authors made theoretical evaluations to rationally link these parameters. For instance, Konrad and Law [27] derived an analytical expression to evaluate  $\sigma'_p$  during cone penetration based on measured piezocone parameters, effective strength parameters and cone roughness. Some authors [11,12,15] combined Spherical Cavity Expansion theory and Critical State Soil Mechanics concepts to link  $OCR$  with normalized CPTU parameters. The link between  $OCR$  and CPTU parameters can be further explained by the strong relation that exists between  $OCR$  and undrained shear strength of clays  $s_u$ , as suggested by the SHANSEP approach [2]. As the  $s_u$  is linked to the CPTU parameters by a bearing capacity theory, it is logical to relate  $OCR$  to the same parameters, as suggested by e.g. [28].

In general, published literature correlations follow the format represented by Eq 1 as follows:

$$Y_i = k_j X_j^{\alpha_j} \quad (1)$$

where  $Y_i = \{Y_1, Y_2\} = \{\sigma'_p, OCR\}$ ,  $X_j = \{X_1, \dots, X_7\}$  are the measured or derived CPTU parameters and  $k_j$ ,  $\alpha_j$  the regression coefficients relative to the different parameters as described in Table 3. Table 3 summarizes typical values of  $k_j$  and  $\alpha_j$  from the literature for different types of correlations.

Powell et al. [24] concluded that the linear relationship ( $\alpha_j = 1$ ) between  $\sigma'_p$  and  $q_{net}$  or  $OCR$  and  $Q_t$  seems to be the most reliable. They observed  $k_l$  (or  $k_d$ ) to be clay or site-dependent and measured values between 0.2 and 0.5 for normally to medium overconsolidated clays ( $OCR < 5$ ). Based on a large data set consisting of 205 clay sites all over the world, Chen and Mayne [13] suggested  $k_l = 0.31$  with a coefficient of determination  $r^2 = 0.82$ . They further observed how correlations to  $\sigma'_p$  resulted in higher  $r^2$  compared to correlations to  $OCR$ . For Eastern Canada clays, Leroueil et al. [25] proposed  $k_l = 0.28$ . For organic soft clays and silts, Mesri [26] recommended  $k_l = 0.24$ . Mayne [15] proposed  $k_l = 0.33$  for clays with  $OCR < 3$ , based on an analytical solution that combines Spherical Cavity Expansion theory and Critical State Soil Mechanics. Mayne and Holz [12] further observed that a good non-linear correlation existed between  $OCR$  and  $Q_u$ . Moreover, Chen and Mayne [13] and Schroeder et al. [23] suggested  $OCR$  to be dependent on  $B_q$ , decreasing with increasing  $B_q$ .

Figures 2 and 3 show a comparison between the CLAY/9/249 database and some of the existing correlations for  $\sigma'_p$  and  $OCR$  respectively. The uncertainties of the existing correlations associated with the CLAY/9/249 database are evaluated by calculating the bias factor ( $b$ ) and coefficient of variation ( $COV$ ) according to Ching and Phoon [16]. The bias factor  $b$  is defined as the mean value of the ratio (measured  $OCR$ )/(calculated  $OCR$ ) or (measured  $\sigma'_p$ )/(calculated  $\sigma'_p$ ). If  $b = 1$ , the prediction is unbiased. The  $COV$  is calculated as the ratio of the standard deviation of the (measured  $OCR$ )/(calculated  $OCR$ ) ratio and the bias factor  $b$ . If  $COV$  tends to zero, low variability is expected around the mean trend of the data. Calculated  $b$  and  $COV$  for the existing correlations in Figures 2 and 3 are summarized in Table 4.

**Table 3.** Literature summary of calibration parameters for  $\sigma'_p$  and  $OCR$  from Eq 1.

Target parameter ( $Y_i$ )		CPTU parameter ( $X_j$ )		Coefficient $k_j$		Coefficient $\alpha_j$		Source
$Y_1$	$\sigma'_p$	$X_1$	$q_{net}$	$k_1$	0.24–0.40	$\alpha_1$	1.0	[13,25,29]
$Y_1$	$\sigma'_p$	$X_2$	$\Delta u$	$k_2$	0.53–0.54	$\alpha_2$	1.0	[13,15]
$Y_1$	$\sigma'_p$	$X_3$	$q_e$	$k_3$	0.50–0.60	$\alpha_3$	1.0	[13,15]
$Y_2$	$OCR$	$X_4$	$Q_t$	$k_4$	0.20–0.50	$\alpha_4$	1.0–1.2	[14,24]
$Y_2$	$OCR$	$X_5$	$Q_u$	$k_5$	0.31	$\alpha_5$	1.35	[12]
$Y_2$	$OCR$	$X_6$	$Q_e$	$k_6$	0.5–0.545	$\alpha_6$	0.97–1.0	[10,13]
$Y_2$	$OCR$	$X_7$	$B_q$	$k_7$	0.63–1.026	$\alpha_7$	–1.077/–1.286	[13,23]

According to Table 4, all the correlations seem to overpredict the mean trend of the data in CLAY/9/249, except for the expression by Schroeder et al. [23], which underpredicts the mean trend. In particular, the correlations by Chen and Mayne [13] for  $\sigma'_p$  seem to capture the upper boundary of the data points in CLAY/9/249, as shown in Figure 2. The existing  $Q_t - OCR$  and  $Q_e - OCR$  correlations seem to deviate significantly from the mean trend of the data points. On the other hand, the  $Q_u - OCR$  and  $B_q - OCR$  relations by Mayne and Holtz [12] and Chen and Mayne [13], respectively, appear to better fit the data trend in CLAY/9/249. Overall, the linear  $q_{net} - \sigma'_p$  and  $Q_t - OCR$  relations seem to be characterized by the lowest uncertainties (lowest  $COV = 0.20$  in Table 4). This is in line with the experimental observations by Powell et al. [24].

**Table 4.** Bias and uncertainties of the existing correlations associated with CLAY/9/249 database.

Correlation	Source	$b$	$COV$
$\sigma'_p = 0.305q_{net}$	Chen and Mayne [13]	0.80	0.20
$\sigma'_p = 0.53\Delta u$	Chen and Mayne [13]	0.81	0.22
$\sigma'_p = 0.50q_e$	Chen and Mayne [13]	0.92	0.35
$OCR = 0.317Q_t$	Chen and Mayne [13]	0.77	0.20
$OCR = 0.259Q_t^{1.107}$	Chen and Mayne [13]	0.78	0.22
$OCR = (Q_t/3)^{1.2}$	Karlsrud et al. [14] ( $S_t > 15$ )	0.63	0.24
$OCR = (Q_t/2)^{1.1}$	Karlsrud et al. [14] ( $S_t < 15$ )	0.44	0.22
$OCR = 0.314Q_u^{1.35}$	Mayne and Holtz [12]	0.86	0.26
$OCR = 0.545Q_e^{0.969}$	Chen and Mayne [13]	0.88	0.34
$OCR = 1.026B_q^{-1.077}$	Chen and Mayne [13]	0.90	0.25
$OCR = 0.63B_q^{-1.286}$	Schroeder et al. [23]	1.31	0.28

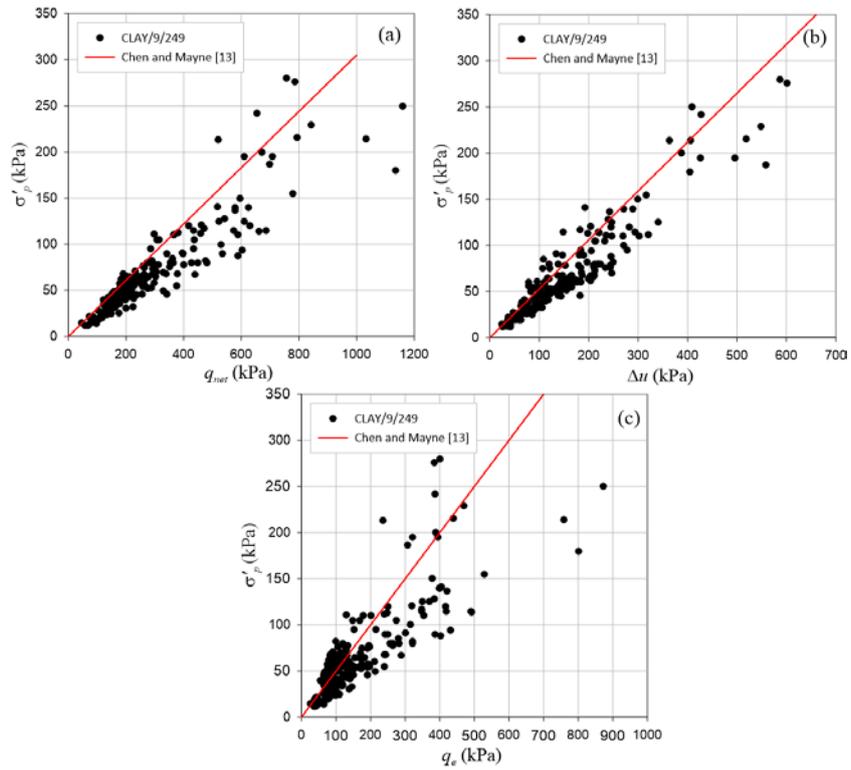


Figure 2. Comparison of CLAY/9/249 database with existing correlations for  $\sigma'_p$ .

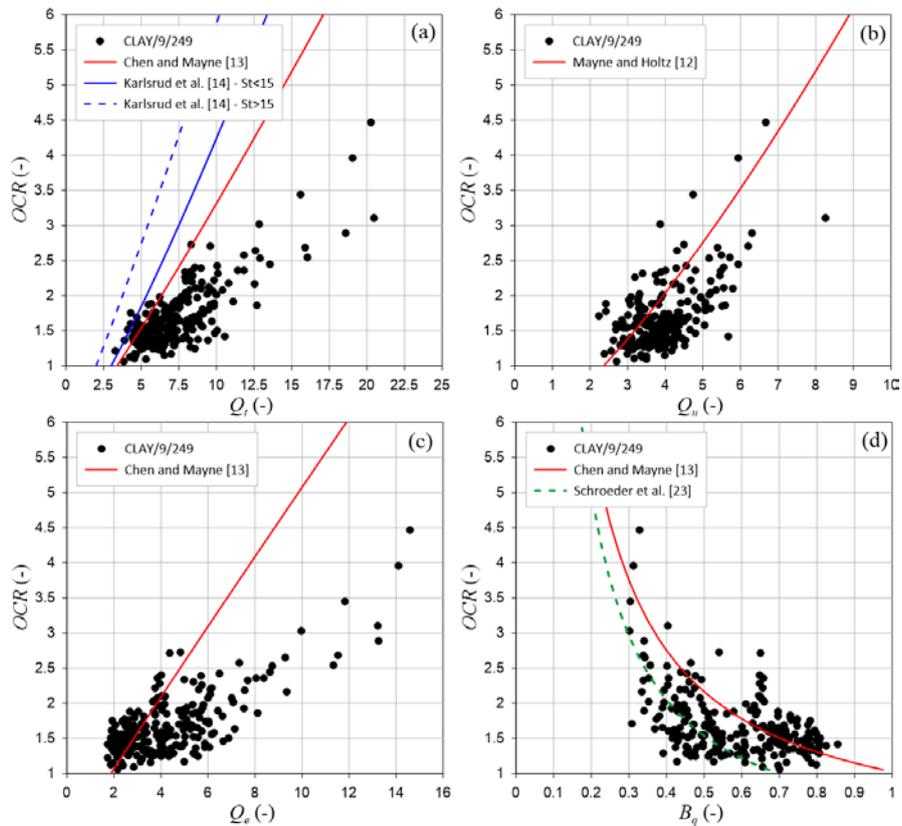


Figure 3. Comparison of CLAY/9/249 database with existing correlations for OCR.

#### 4. CPTU-based correlations for $\sigma'_p$ and $OCR$ from CLAY/9/249 database

The compiled CLAY/9/249 database is used to derive improved CPTU-based correlations for  $\sigma'_p$  and  $OCR$  by means of linear regression analyses. Besides simple linear regression, multivariable regression is considered in order to maximize the coefficient of determination  $r^2$ .

The linear dependence between  $\sigma'_p$ ,  $OCR$  and CPTU and index parameters is studied through the Pearson's correlation coefficient. The Pearson's correlation coefficient is a measure of the linear dependence (or correlation) between two variables. It has a value between +1 and -1, where 1 suggests total positive linear correlation, 0 no linear correlation, and -1 total negative linear correlation. As shown in Table 5, the strongest linear correlations are between  $\sigma'_p$  and  $q_{net}$ ,  $\sigma'_p$  and  $\Delta u$  and  $OCR$  and  $Q_t$ . A weak linear correlation seems to exist between  $\sigma'_p$ ,  $OCR$  and index parameters. This confirms the findings of Yang et al. [19].

**Table 5.** Pearson's correlation coefficient for different pairs of variables.

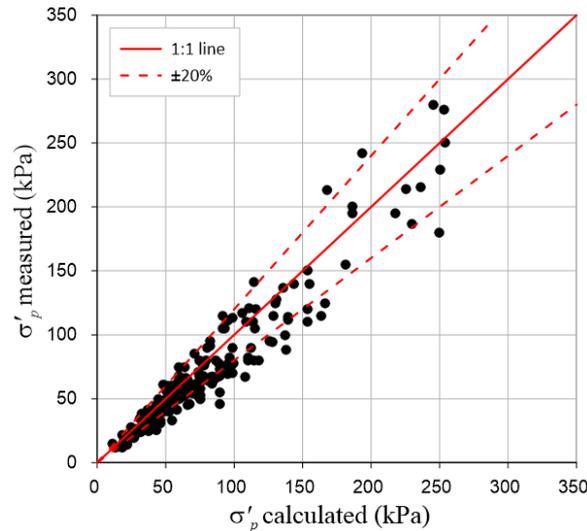
Parameter	$q_{net}$	$\Delta u$	$q_e$	$Q_t$	$Q_u$	$Q_e$	$B_q$	$I_p$	$w$	$S_t$
$\sigma'_p$	0.91	0.94	0.82	-	-	-	-	-0.15	-0.42	-0.10
$OCR$	-	-	-	0.81	0.59	0.76	-0.48	0.09	-0.17	-0.04

Table 6 presents the best-fit correlations from linear regression analyses. Following the indications of Table 5, the highest  $r^2$  values in Table 6 are found between  $\sigma'_p$  and a combination of  $q_{net}$  and  $\Delta u$ . In general, correlations to  $\sigma'_p$  are characterized by higher  $r^2$  compared to correlations to  $OCR$ . This is consistent with the observations made by Chen and Mayne [13]. The highest  $r^2$  (= 0.93) was found for Eq 2 from a multivariable linear regression analysis between  $\sigma'_p$  and two variables,  $q_{net}$  and  $\Delta u$ . By adding further variables to Eq 2, the calculated  $r^2$  does not increase significantly. Figure 4 shows a comparison between the measured and calculated  $\sigma'_p$  values from Eq 2. The majority of the data is within the  $\pm 20\%$  boundaries.

$$\sigma'_p/p_a = 0.313(q_{net}/p_a)^{0.514}(\Delta u/p_a)^{0.511} \quad (2)$$

**Table 6.** Best-fit correlations for CLAY/9/249 database.

Correlation	Type	$r^2$
$\sigma'_p = 0.24q_{net}$	Linear	0.83
$\sigma'_p = 0.43\Delta u$	Linear	0.88
$\sigma'_p = 0.37q_e$	Linear	0.60
$OCR = 0.705 + 0.136Q_t$	Linear	0.66
$OCR = 0.385 + 0.327Q_u$	Linear	0.35
$OCR = 1.04 + 0.152Q_e$	Linear	0.57
$OCR = 1.261B_q^{-0.462}$	Power	0.26
$\sigma'_p/p_a = 0.313(q_{net}/p_a)^{0.514}(\Delta u/p_a)^{0.511}$	Power (multivariable)	0.93



**Figure 4.** Comparison of measured vs calculated  $\sigma'_p$  from Eq 2.

## 5. Discussion

As discussed in the previous sections, several correlations exist in the literature for modeling stress history of clays from CPTU. This paper contributes to the geotechnical literature with new correlations and a high-quality database.

Sample quality clearly affects CPTU calibration and, therefore, correlations. The quality of the data used to derive correlations may vary significantly among the different literature sources. In these studies, sample quality is rarely discussed and, therefore, a possibility exists that the calibration data is not of high quality. In addition, even samples that are evaluated as “very good to excellent” according to Lunne et al.’s [5] criterion may not be of the highest quality. For instance, L’Heureux et al. [30] compared 72 mm piston and 250 mm block samples from Rakkestad sensitive clay in Southern Norway and observed how the block samples resulted in higher  $\sigma'_p$  and undrained shear strength, despite the comparable assessed sample quality. The data in the CLAY/9/249 database is considered to be of the best possible quality, especially in relation to the offshore data. That said, samples will still be characterized by a degree of disturbance that cannot be easily quantified.

One of the outcomes of the regression analyses (Table 6) is that the best relationship exists between  $\sigma'_p$  and a combination of  $q_{net}$  and  $\Delta u$ . In practice, the relationship between  $\sigma'_p$  and  $q_{net}$  is the one that is most commonly used, especially in offshore geotechnics. The relationship between  $OCR$  and  $Q_t$  is used in the same way, according to Eq 3.

$$k_1 = \frac{\sigma'_p}{q_{net}} = \frac{OCR}{Q_t} = k_4 = k \quad (3)$$

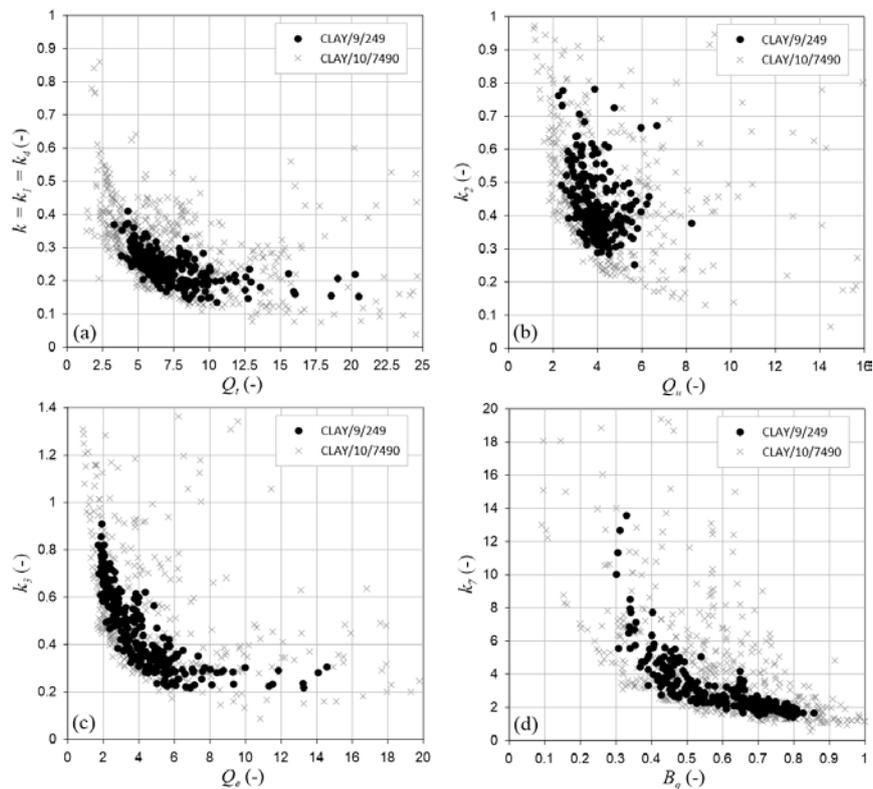
In absence of site-specific data, the coefficient  $k = k_1 = k_4$  is often taken equal to 0.3, as suggested, for instance, by Chen and Mayne [13]. In this study,  $k = 0.24$  was found. Indirectly, this study demonstrated that there is a weak correlation between  $k_j$  values and index properties. However, besides the site-dependency and the natural variability of soil properties, assuming a constant value of  $k_j$  may not always be a safe choice. Figure 5a plots  $k$  versus  $Q_t$  from the CLAY/9/249 database. The coefficient  $k$  shows a non-linear variation with  $Q_t$ , decreasing with increasing  $Q_t$ . For  $Q_t > 10$ ,  $k$

appears to become fairly constant. Similar behavior is observed with respect to  $\Delta u$  ( $k_2$ ),  $q_e$  ( $k_3$ ) and  $B_q$  ( $k_7$ ), as shown in Figure 5b–5d. Despite the scatter, there is an indication that  $k_j = \text{constant}$  can be assumed when the normalized CPTU parameters (e.g.,  $Q_t$ ) vary within a reasonably small interval. This aspect becomes relevant especially in offshore clays that have been subjected to ice loading. In these cases, the normalized CPTU parameters may vary significantly with depth. Therefore, assuming  $k_j = \text{constant}$  may lead to a non-conservative solution.

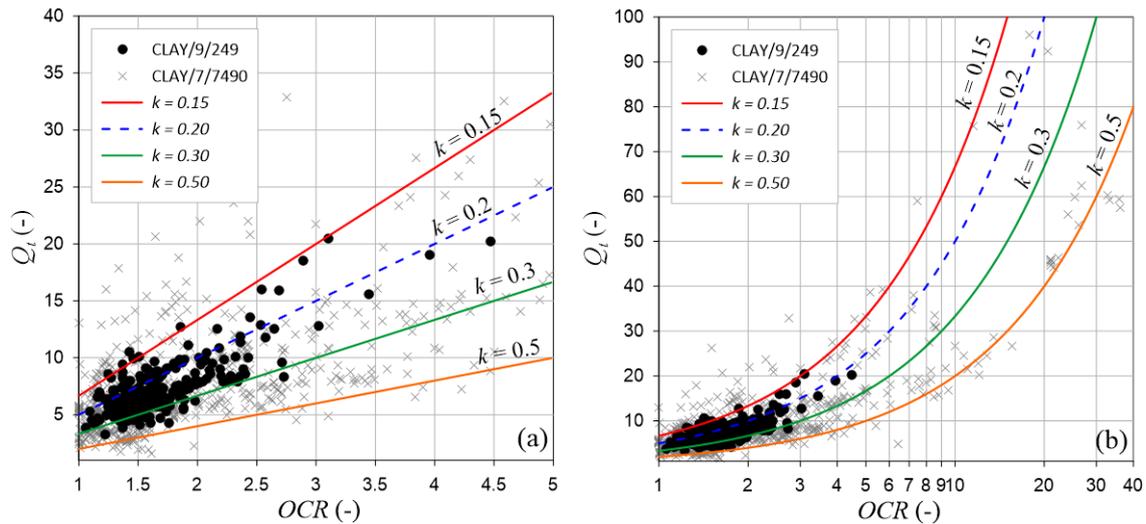
The data in CLAY/9/249 covers  $OCR$  values  $\sim 1$  to 5. The correlations and the recommendations given in this study should be then used carefully in presence of  $OCR$ s greater than 5. As discussed in Powell et al. [24], pore pressure measurements should not be used in heavily overconsolidated clays, where  $B_q$  can become very small or even negative.

Figure 5 further compares the CLAY/9/249 database with the large CLAY/10/7490 database compiled by Ching and Phoon [16]. Despite the high scatter, the large database shows similar trends as the CLAY/9/249 database.

Figure 6 illustrates Eq 3 for different values of  $k$ . The theoretical curves are compared with the data points in the CLAY/9/249 and CLAY/10/7490 databases. The lower and upper boundaries of  $k_1$  can be identified at  $k \sim 0.15$  and  $k \sim 0.40$ , respectively. Furthermore,  $k \sim 0.15$ – $0.5$  seems to cover the majority of the data points in the CLAY/10/7490 database, which includes  $OCR$ s up to  $\sim 40$ . For onshore Norwegian clays, Paniagua et al. [31] found  $k \sim 0.2$ – $0.75$  based on high-quality block sample data with  $OCR \sim 1$ – $7$ . Based on the Authors' experience, data points for which  $k$  is less than 0.15 are likely to suffer of severe sample disturbance.



**Figure 5.** Variation of  $k$  ( $= k_1 = k_4$ ),  $k_2$ ,  $k_3$  and  $k_7$  with normalized CPTU parameters.



**Figure 6.**  $Q_t$  –  $OCR$  relationship and variability of the coefficient  $k$ .

## 6. Conclusions

This paper presents a multivariate database consisting of 249 high-quality onshore and offshore clay data points, labeled as CLAY/9/249 database. The database covers a wide range of basic clay parameters and  $OCR$  between 1 and 5. The new database is exploited to derive CPTU-based correlations for stress history of clays. Existing correlations are compared to the database and their uncertainties are quantified. The trends observed from the new data are confirmed by the existing large CLAY/10/7490 database [16]. In general, some of the new correlations in the present study have lower uncertainties than the majority of those proposed in the literature.

One of the main results of this study is that the relationship between  $\sigma'_p$  and a combination of  $q_{net}$  and  $\Delta u$  is characterized by a lower variability than the relationship between  $OCR$  and the normalized CPTU parameters. However, despite the high quality of the data points, correlations are still affected by uncertainties, which could not be justified by the variability in the index parameters. Therefore, the correlations proposed in this study should be used only for preliminary assessment of the in-situ stress history in the absence of site-specific data, or for comparison when the available data is limited or suspected to be unreliable.

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## Conflict of interest

The authors declare no conflict of interest.

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